



KCM ENGINEERING

TRILLIUM RAILWAY SHORING & HWY 406 WIDENING MTO 2011-2005

ANCHORED SHORING DESIGN DOCUMENTATION

Soldier pile with tie shoring

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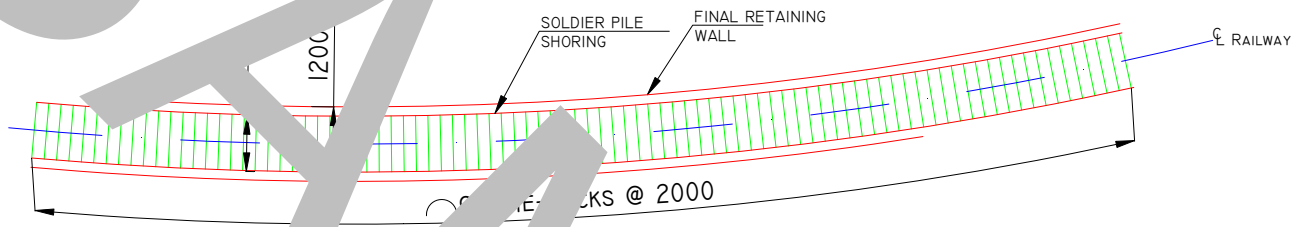


ANCHORED SOLDIER PILE (Anchor depth: 1.5 m)

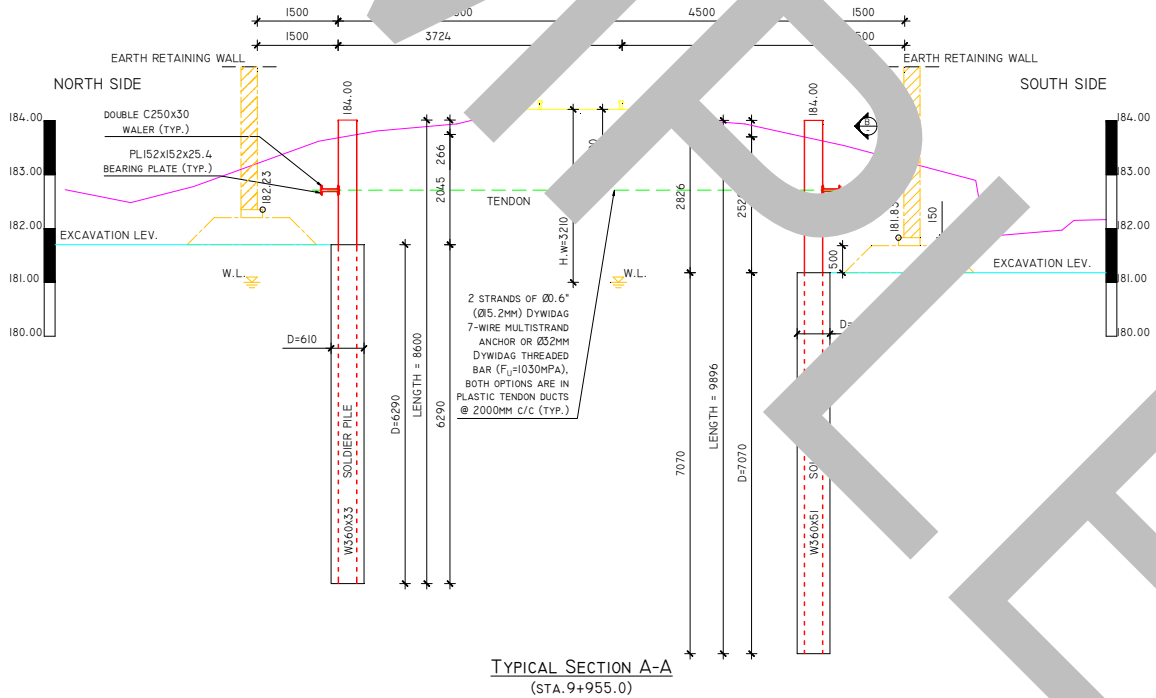
1. Input parameters

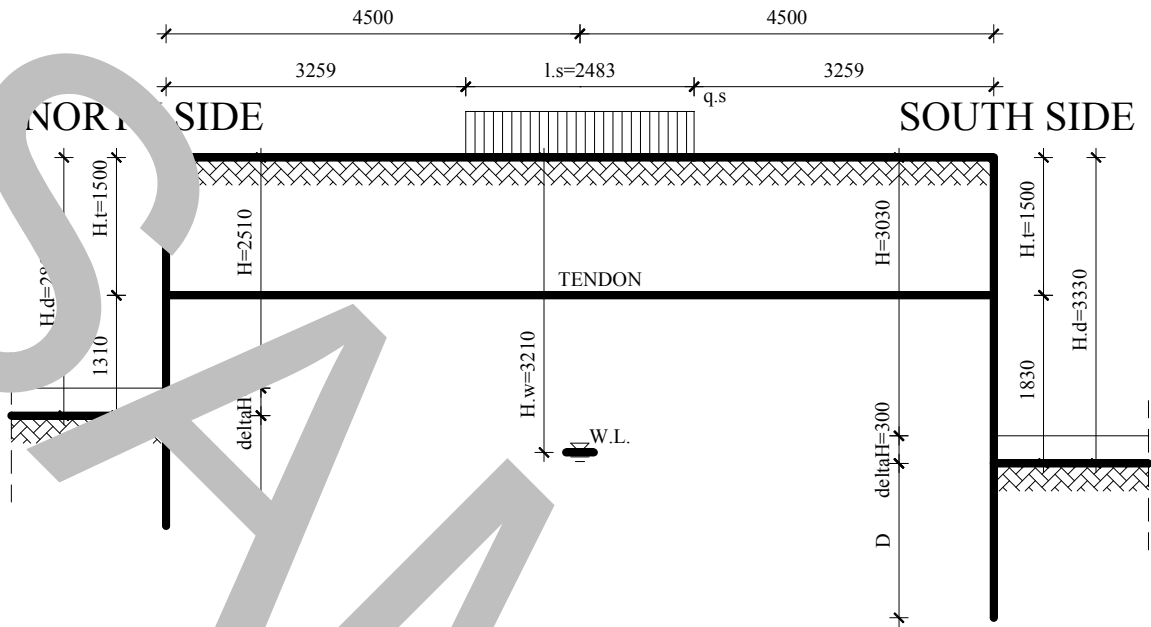
1.1. Geometry

1.1.1. Plan view



1.1.2. Cross section @ 9+955





The first element of the vectors refers to the north side, the second to the southern side of the railway.

Height from top of the soldier pile to bottom of excavation: $H_t = \begin{pmatrix} 2.51 \\ 3.02 \end{pmatrix}$

Uncertainty in the depth of excavation: $\Delta H = 0.51 \text{ m}$

Design height of excavation from top of the soldier pile: $H_d = H + \Delta H = \begin{pmatrix} 2.81 \\ 3.33 \end{pmatrix}$

Depth of the tendon: $H_t := 1.5 \text{ m}$ "Design Criteria" 11. 12. 13. pts.

Based on the documents provided by Terraprobe Inc. the water level is at the elevation of 100m, this is a temporary state, therefore an assumed surplus of 1 m will be used.

Depth of water level from top of the soldier pile: $H_w := 3.21 \text{ m}$

Width of the track (tie length): $l_s := 8 \text{ ft} = 2.438 \text{ m}$ "Design Criteria" 9

At passive earth pressure side, tributary width of caissons is taken as double of diameter of caisson (2Φ), according to AREMA 28.5.3.2.



1.2. Standards, regulations

AREMA Part 20 - Flexible Sheet Pile Bulkheads
 AREMA Part 20 - Temporary Structures for Construction

For soldier piles with timber lagging:
 Temporary Shoring Design Load Diagrams
 Temporary Shoring Construction Procedure
 Design Criteria 10. pt. 11. Jan. 06.

1.3. Material properties

1.3.1. Soil

Cinder fill material with organics overlaying silty clay.

Passive earth pressure coefficient: $K_p := 3$

The given data apply to the soldier pile type of construction. The Temporary Shoring Design Load Diagrams and the "Design Criteria 10.pt." indicate that on the retained side **instead of the active earth pressure the at rest earth pressure** (which is greater in magnitude) should be applied, with a minimum coefficient of 0.5. Further on this assumption will be used, however in other respects the regulations of AREMA Part 20 will be adapted.

At rest earth pressure coefficient: $K_0 := 0.5$

"Design Criteria"
10.pt.

Unit weight of the moist soil: $\gamma_{\text{moist}} := 20.7 \frac{\text{kN}}{\text{m}^3}$

Unit weight of submerged soil (**assumed**): $\gamma_{\text{sub}} := 21 \frac{\text{kN}}{\text{m}^3}$

1.3.2. Water

Unit weight of water: $\gamma_w := 10 \frac{\text{kN}}{\text{m}^3}$

1.3.3. Tendon

In **this case** (notably when the anchor is 1.5 m below the rail) the **tendon** type given in the Temporary Shoring Construction Procedure will be utilized.

Dywidag Multistrand

- 0.6" dia. (15.24 mm),
- 7-wire,
- 270 ksi (1862 MPa),
- Low relaxation,
- Greased and coated,
- Conforming to CSA G279-87 (ASTM A 416)

"Design Criteria"
10.pt.



Data provided by the manufacturer:

Minimum ultimate strength:

$$f_{pu} := 270 \text{ ksi} = 1862 \cdot \text{MPa}$$

(based on provided construction procedure)

Nominal cross section area per strand:

$$A_s := 0.217 \text{ in}^2 = 140 \cdot \text{mm}^2$$

Ultimate strength of a strand:

$$F_{pu} := f_{pu} \cdot A_s = 261 \cdot \text{kN}$$

Maximum jacking force:

$$F_{pj} := 0.8 F_{pu} = 208 \cdot \text{kN}$$

Maximum jacking force:

$$F_{pl} := 0.7 F_{pu} = 182 \cdot \text{kN}$$

Note: the tendons are rounded, and curved at the two sides.

"Design Criteria"
14. 22.6. 22.8.pt

1.3.4. Steel soldier pile

Yield stress:

$$F_y := 350 \text{ MPa}$$

Young modulus:

$$E_s := 200 \text{ GPa}$$

1.4. Safety factors

Soldier pile tensile yield strength: (AREMA 8-20.5.3.1)

$$FS_{sp} := \frac{2}{3} = 0.67$$

Anchor allowable stress: (AREMA 8-20.5.7.a(2).)

$$FS_{anch} := 1.5$$

"Design Criteria"
16.pt.

Passive resistance: (AREMA 8-28.5.1.2.)

$$FS_{pr} := 1.5$$

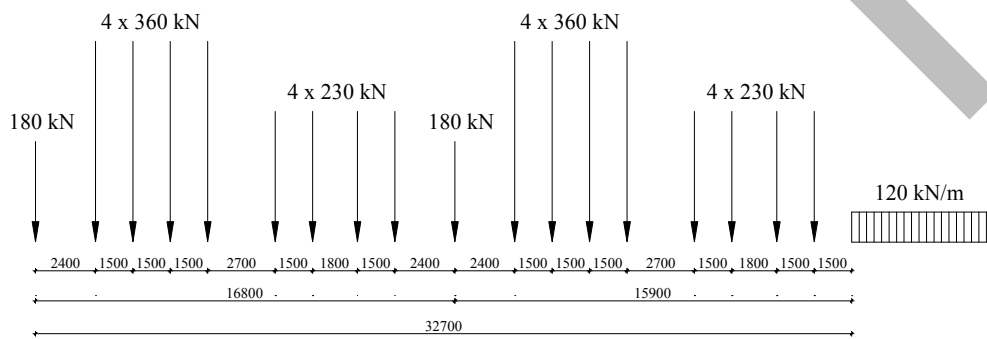
"Design Criteria"
21.pt.

1.5. Loads

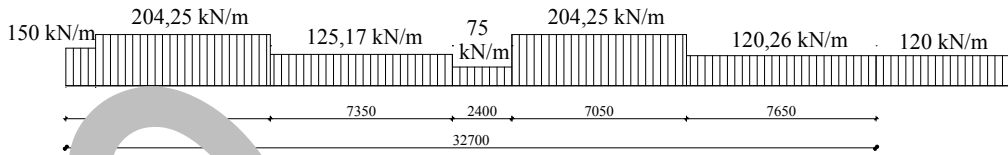
1.5.1. Live loads

1.5.1.1. Vertical

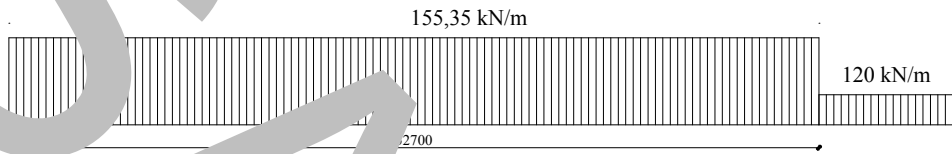
The vertical live load is the Cooper E 90, which is equal to the Cooper E 80 (EM 36) multiplied by 1.125. The Cooper E 80 can be found in AREMA Part 28, fig. 8-2-1. as follows:



These axial loads can be considered as distributed loads due to the effect of the substructure of the railway. Let's take first the approximation of coupling the similar axial loads:



If we distribute all the above loads along the length of the carriage, we get:



According to the "Design Criteria" 9 the applied strip load magnitude is the following:

The strip load (Cooper E90, AASHTO 1010):
$$\frac{90 \text{ kip}}{5 \text{ ft} \cdot l_s} = 107.731 \cdot \text{kPa}$$

"Design Criteria"
9.pt.

1.5.1.2. Horizontal

from the Boussinesque solution:

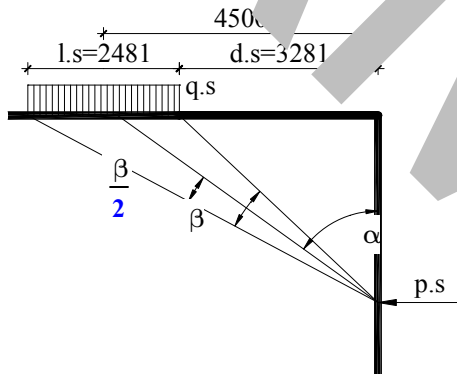
$$p_s = \frac{2 \cdot q_s}{\pi} \cdot \left[\beta + \sin(\beta) \cdot (\sin(\alpha))^2 - \sin(\beta) \cdot (\cos(\alpha))^2 \right]$$

Change into cartesian coordinates:

$$\alpha = \frac{1}{2} \cdot \left(\frac{d_s + l_s}{z} - \frac{d_s}{z} \right)$$

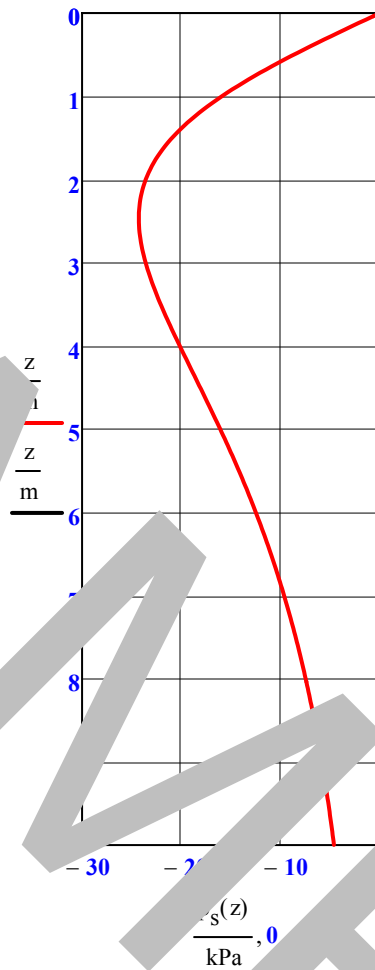
$$\beta = \frac{1}{2} \cdot \left(\text{atan} \left(\frac{d_s + l_s}{z} \right) - \text{atan} \left(\frac{d_s}{z} \right) \right)$$

$$l_s = 2481 \text{ m} \quad d_s = 3281 \text{ m} \quad z = 3.281 \text{ m}$$



The horizontal strip load as the function of the depth:

$$p_s(z) := \begin{cases} 0 & \text{if } z = 0 \\ \frac{2 \cdot q_s}{\pi} \cdot \left[\text{atan} \left(\frac{d_s + l_s}{z} \right) - \text{atan} \left(\frac{d_s}{z} \right) \right] + \sin \left(\text{atan} \left(\frac{d_s + l_s}{z} \right) - \text{atan} \left(\frac{d_s}{z} \right) \right) \cdot \left[\sin \left[\frac{1}{2} \cdot \left(\text{atan} \left(\frac{d_s + l_s}{z} \right) + \text{atan} \left(\frac{d_s}{z} \right) \right) \right]^2 + \cos \left[\frac{1}{2} \cdot \left(\text{atan} \left(\frac{d_s + l_s}{z} \right) + \text{atan} \left(\frac{d_s}{z} \right) \right) \right]^2 \right] & \text{otherwise} \end{cases}$$



The horizontal pressure from Cooper E90 live load acting on the shoring



2. NORTHERN SIDE

2.1. Fundamental dead loads - northern side

2.1.1. Functions

Retained soil $H_d = 1.5 \text{ m}$ Tributary area of a pile: $X := 2 \text{ m}$

At rest earth pressure

$$p_{z,e}(z) := \begin{cases} 0 \cdot \gamma_{\text{moist}} \cdot z & \text{if } z < H_w \\ -K_0 \cdot [\sigma_{\text{subm}} - \gamma_w + (\gamma_{\text{subm}} - \gamma_w) \cdot (z - H_w)] & \text{otherwise} \end{cases}$$

Water pressure

$$u_0(z) := \begin{cases} 0 & \text{if } z < H_w \\ -\gamma_w \cdot (z - H_w) & \text{otherwise} \end{cases}$$

Resisting side

Passive earth pressure

According to the "Design Criteria" (20.pt.) the passive resistance of the soil is considered within a width at least 1.5 times the pile width.

Pile width:

$$\begin{aligned} \Phi &= 0.61 \text{ m} \\ \Delta_p &:= 1.5 \cdot \Phi = 0.915 \text{ m} \end{aligned}$$

"Design Criteria"
20.pt.

$$p_{z,p}(z) := \frac{1}{FS_{rp}} \cdot \begin{cases} 0 & \text{if } z < H_{d1} + \Delta_p \\ K_p \cdot (\gamma_{\text{subm}} - \gamma_w) \cdot [z - (H_{d1} + \Delta_p)] & \text{otherwise} \end{cases}$$

"Design Criteria"
21.pt.

Water pressure

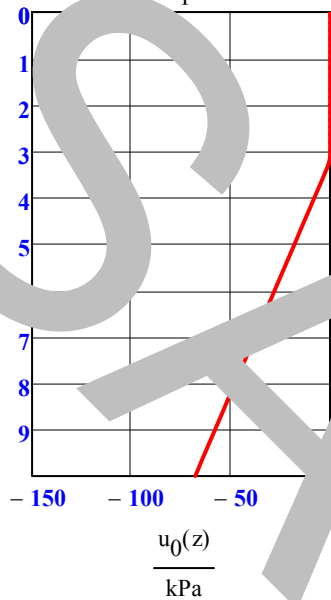
$$u_p(z) := \begin{cases} 0 & \text{if } z < H_{d1} + \Delta_p \\ \gamma_w \cdot [z - (H_{d1} + \Delta_p)] & \text{otherwise} \end{cases}$$



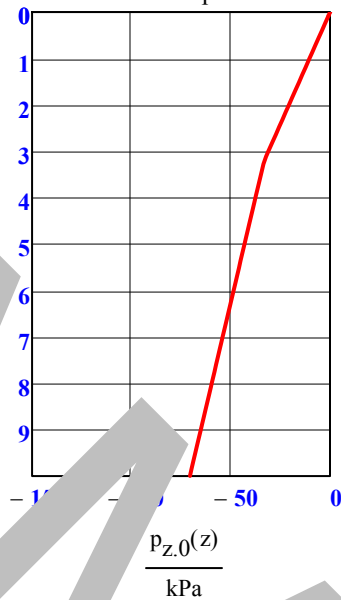
2.1.2. Graphs

Retained side

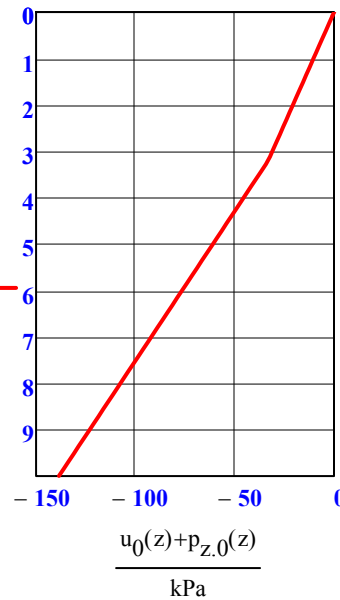
Water pressure



At rest earth pressure

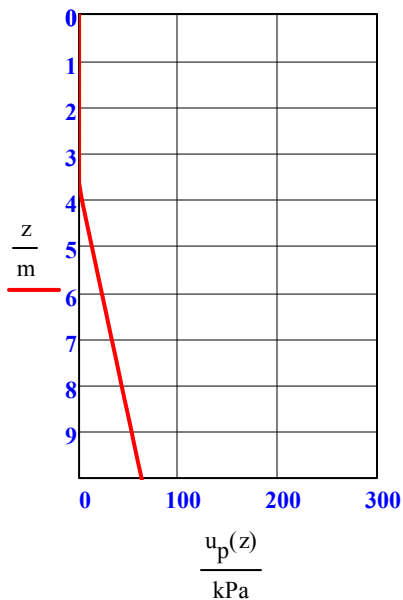


At rest earth pressure +
Water pressure

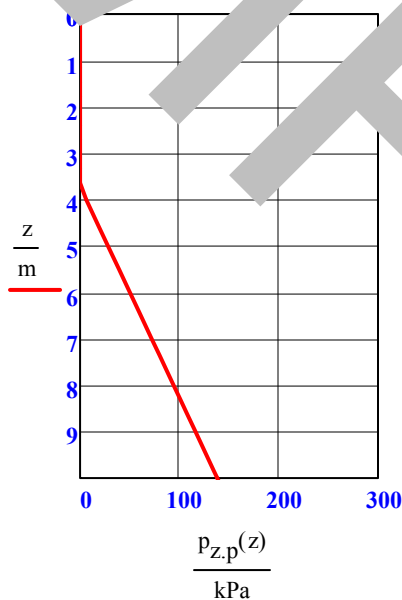


Resisting side

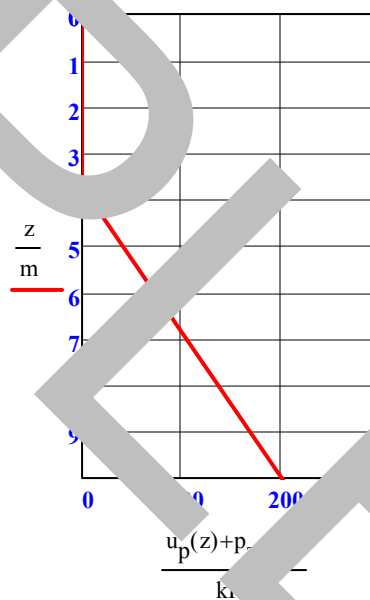
Water pressure



Passive earth pressure



Passive earth pressure +
Water pressure





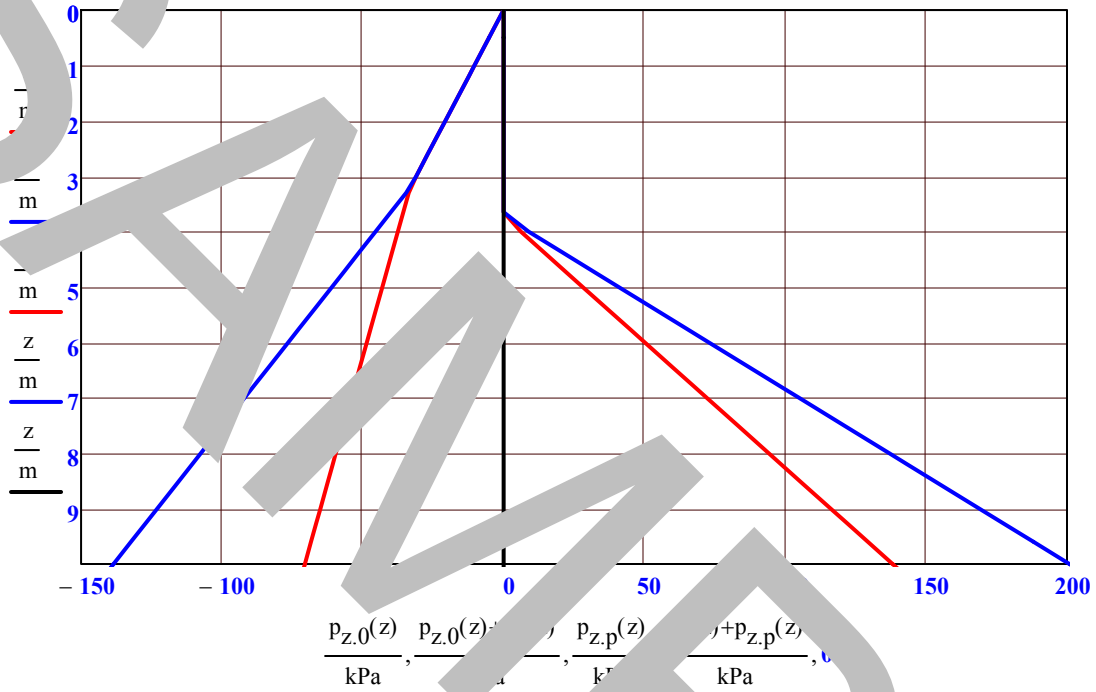
In a joint diagram

Retained side

Resisting side

Blue: At rest earth pressure +
Water pressure
Red: At rest earth pressure

Blue: Passive earth pressure +
Water pressure
Red: Passive earth pressure





2.2. Design calculation - northern side

2.2.1. Figure of horizontal loads

Pressure on the retained side:

$$ret(z) := p_{z,0}(z) + u_0(z) + p_s(z)$$

Pressure on the resisting side:

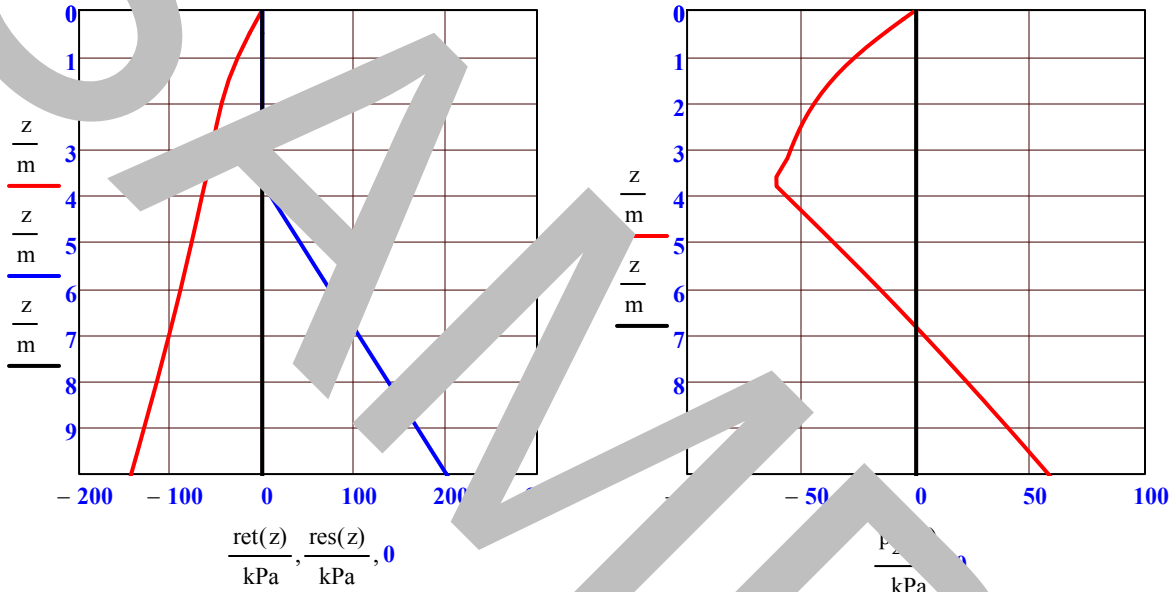
$$res(z) := p_{z,p}(z) + u_p(z)$$

Resultant of the two actions:

$$p_{\Sigma}(z) := res(z) + ret(z)$$

Retained side Resisting side

The sum of the pressures acting on the wall.



The depth at which the pressure becomes zero: $z_1 = \text{root}(p_{\Sigma}(z)) = 6.834 \text{ m}$

2.2.2. Depth of embedment

2.2.2.1. Anchor force (horizontal equilibrium)

The force in the anchor equals to the negative resultant of the distributed loads:

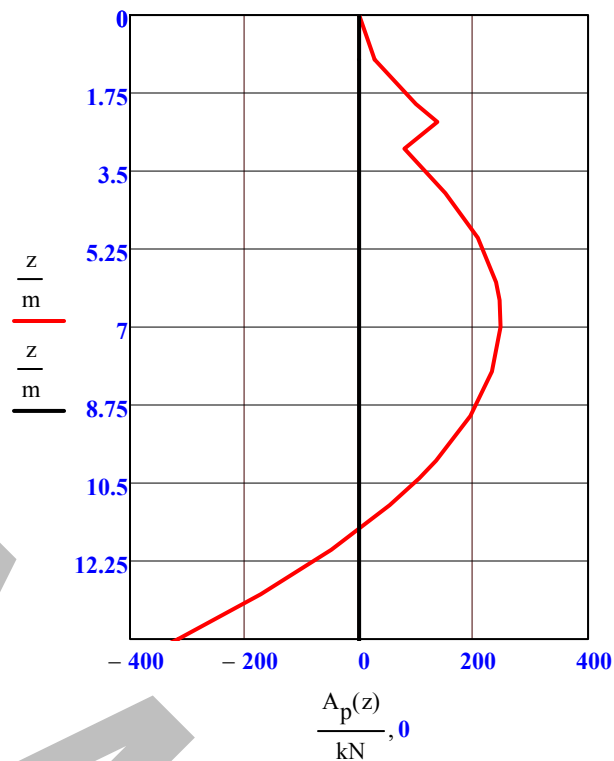
$$A_p(z) := \begin{cases} \left[-\int_0^z p_{\Sigma}(t) dt \right] \cdot X & \text{if } z \leq H_1 \\ \left[-\int_0^{H_1} p_{\Sigma}(t) dt \right] \cdot X - \left[\int_{H_1}^{z_1} p_{\Sigma}(t) dt \right] \cdot \Phi - \left[\int_{z_1}^z p_{\Sigma}(t) dt \right] \cdot 2\Phi & \text{if } z > H_1 \end{cases}$$

In the equations "X" denotes tributary width above excavation level, "Φ" denotes width of concrete caisson where at-rest soil pressure is present, "2Φ" denotes equivalent width of concrete caisson where passive soil pressure is present according to AREMA 28.5.3.2.



The depth at which the resultant of the pressures becomes zero:

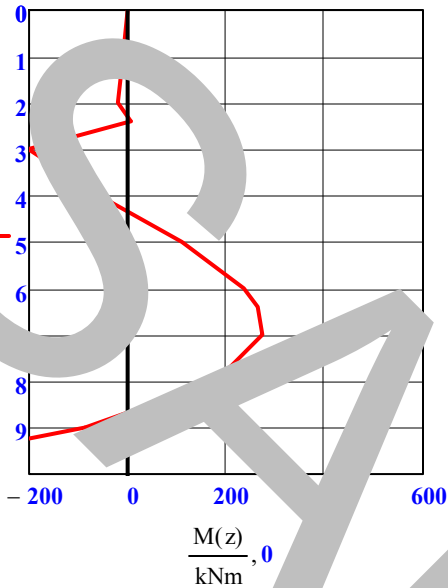
$$z_2 := \text{root}(A_p(\text{var}), \text{var}) = 11.55 \text{ m}$$



2.2.2.2. Depth of embedment (bending moment at the bottom)

The bending moment for a cross section at depth "z":

$$M(z) := \begin{cases} \left[\int_0^z p_{\Sigma}(t)(z-t) dt \right] \cdot X + \begin{cases} 0 & \text{if } z < H_t \\ A_p(z) \cdot (z - H_t) & \text{otherwise} \end{cases} & \text{if } z \leq H_1 \\ \left[\int_0^{H_1} p_{\Sigma}(t) \cdot (z-t) dt \right] \cdot X + \left[\int_{H_1}^{z_1} p_{\Sigma}(t) \cdot (z-t) dt \right] \cdot \Phi + \left[\int_{z_1}^z p_{\Sigma}(t) \cdot (z-t) dt \right] \cdot \Phi + A_p(z) \cdot (z - H_t) & \text{if } z > H_1 \end{cases}$$



Length of soldier pile equals to the coordinate where $M(z)$ becomes zero:

$$L_{w_1} := \text{root}(M(\text{var}), \text{var}) = 8.745 \text{ m}$$

Applied wall length:

$$L_{\text{app.w}_1} := \text{ceil}\left(\frac{L_{w_1}}{0.1\text{m}}\right) \cdot 0.1\text{m} \quad L_{\text{app.w}_1} = 8.8 \text{ m}$$

Depth of the embedment shall be at least 3m according to the "Design Criteria" (23.pt.):

$$D_1 := \max(L_{\text{app.w}_1} - H_{d_1}, 3\text{m}) \quad D_1 = 5.99 \text{ m} \quad \text{"Design Criteria" 23.pt.}$$

2.2.3. Maximum bending moment

Bending moment:

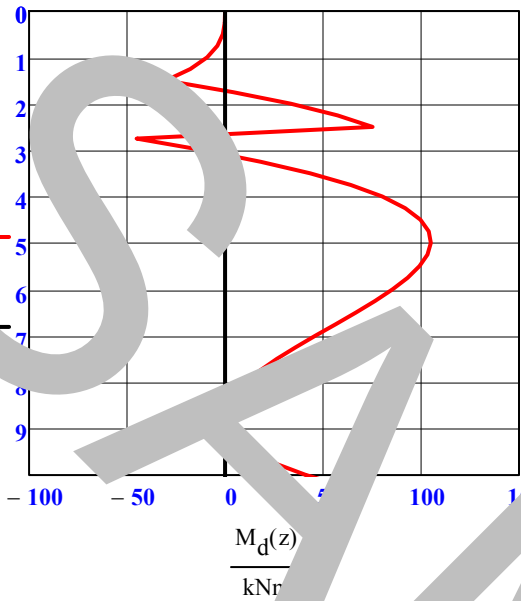
$$M_d(z) := \begin{cases} \left[\int_0^z p_{\Sigma}(t)(z-t) dt \right] \cdot X + \begin{cases} 0 & \text{if } z < H_t \\ A_p(L_{w_1}) \cdot (z - H_t) & \text{otherwise} \end{cases} & \text{if } z \leq H_1 \\ \left[\int_0^{H_1} p_{\Sigma}(t) \cdot (z-t) dt \right] \cdot X + \left[\int_{H_1}^{z_1} p_{\Sigma}(t) \cdot (z-t) dt \right] \cdot \Phi + \left[\int_{z_1}^z p_{\Sigma}(t) \cdot (z-t) dt \right] \cdot 2\Phi + A_p(L_{w_1}) \cdot (z - H_t) & \text{if } z > H_1 \end{cases}$$

Shear force:

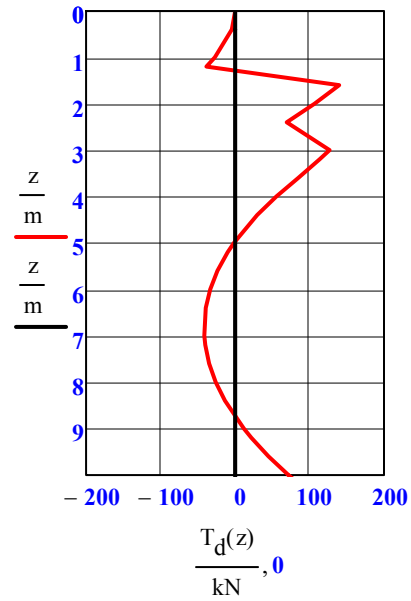
$$T_d(z) := \begin{cases} \left[\int_0^z p_{\Sigma}(t) dt \right] \cdot X + \begin{cases} 0 & \text{if } z < H_t \\ A_p(L_{w_1}) & \text{otherwise} \end{cases} & \text{if } z \leq H_1 \\ \left[\int_0^{H_1} p_{\Sigma}(t) dt \right] \cdot X + \left[\int_{H_1}^{z_1} p_{\Sigma}(t) dt \right] \cdot \Phi + \left[\int_{z_1}^z p_{\Sigma}(t) dt \right] \cdot 2\Phi + A_p(L_{w_1}) & \text{if } z > H_1 \end{cases}$$



Moment diagram



Shear force diagram



The position of the maximum bending moment:

$$z_3 := \text{root}(T_d(\text{var}), \text{var}) = 4.966 \text{ m}$$

The maximum bending moment:

$$M_{\max_1} := M_d(z_3)$$

$$M_{\max_1} = 205 \cdot \text{kNm}$$

Required section modulus:

$$W_{\text{nec}_1} := \frac{M_{\max_1}}{FS_{\text{sp}} F_y}$$

$$W_{\text{nec}_1} = 942.086$$

Applied section: W360x33

Section modulus: $S_{x.360x33} := 474 \cdot 10^3 \text{ mm}^3$

Inertia: $I_{x.360x33} := 82.7 \cdot 10^6 \text{ mm}^4$

Area: $A_{360x33} := 4170 \text{ mm}^2$

2.2.4. Anchor pull

The calculated magnitude:

$$A_1 := A_p(L_{w_1})$$

$$A_1 = 205.953 \cdot \text{kN}$$



The maximum allowable load of a strand:

$$F_{allow} := \frac{F_{pu}}{FS}$$

$$F_{allow} = 130 \cdot \text{kN}$$

"Design Criteria"
16.pt.

Required number of strands per tendon:

$$n_{a1} := \text{ceil}\left(\frac{A_1}{F_{allow}}\right) =$$

$$n_{a1} = 2$$

2.5. Total design load of one tie back

$$F_{pd} := 205.953 \cdot \text{kN}$$

Lock-off load of a tendon (ref.: "Construction Procedure")

$$F_{pl} := 1.1 \cdot F_{pd}$$

$$F_{pl} = 227 \cdot \text{kN}$$

Proof load of a tendon: (ref.: "Construction Procedure")

$$F_{pp} := 1.33 \cdot F_{pd}$$

$$F_{pp} = 274 \cdot \text{kN}$$

2.2.6. Total amount of load on the shoring wall for one-meter length (excavated height)

2.2.6.1. Due to soil

At rest earth pressure:

$$f_{p,0_1} := \int_0^{H_{d1}} p_{z,0}(t) dt = -40.862 \cdot \frac{\text{kN}}{\text{m}}$$

"Design Criteria"
22.1.pt.

2.2.6.2. Due to train load

$$f_{q_1} := \int_0^{H_{d1}} p_s(t) dt = -48.482 \cdot \frac{\text{kN}}{\text{m}}$$

"Design Criteria"
22.2.pt.

2.2.6.3. Due to hydrostatic pressure

$$f_{u_1} := \int_0^{H_{d1}} u_0(t) dt = 0 \cdot \frac{\text{kN}}{\text{m}}$$

"Design Criteria"
22.3.pt.



3. SOUTHERN SIDE

3.1. Horizontal dead loads - southern side

3.1.1. Functions

Retained side: H_{d1} Tributary area of a pile: $X := 2m$

At rest earth pressure

$$p_{z,r}(z) := \begin{cases} K_0 \cdot \gamma_{moist} \cdot z & \text{if } z < H_w \\ -K_0 \cdot [\gamma_{subm} - \gamma_w] \cdot (z - H_w) & \text{otherwise} \end{cases}$$

Water pressure

$$u_0(z) := \begin{cases} 0 & \text{if } z < H_w \\ -\gamma_w \cdot (z - H_w) & \text{otherwise} \end{cases}$$

Resisting side

Passive earth pressure

According to the "Design Criteria" (20.pt.) the active resistance of the soil shall be ignored within a width at least 1.5 times the pile width.

Pile width:

$$\Phi := 1m$$

$$\Delta_p := 1.5 \cdot \Phi = 1.5m$$

"Design Criteria"
20.pt.

$$p_{z,p}(z) := \frac{1}{FS_{rp}} \cdot \begin{cases} 0 & \text{if } z < H_{d2} + \Delta_p \\ K_p \cdot (\gamma_{subm} - \gamma_w) \cdot [z - (H_{d2} + \Delta_p)] & \text{otherwise} \end{cases}$$

"Design Criteria"
21.pt.

Water pressure

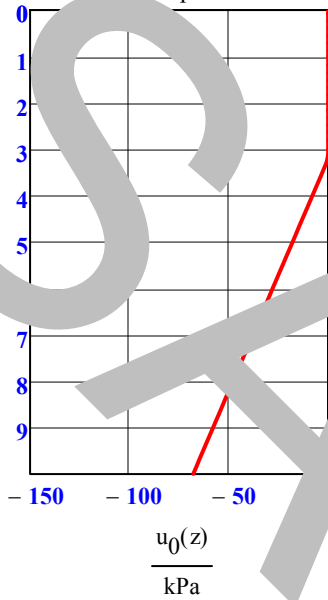
$$u_p(z) := \begin{cases} 0 & \text{if } z < H_{d2} + \Delta_p \\ \gamma_w \cdot [z - (H_{d2} + \Delta_p)] & \text{otherwise} \end{cases}$$



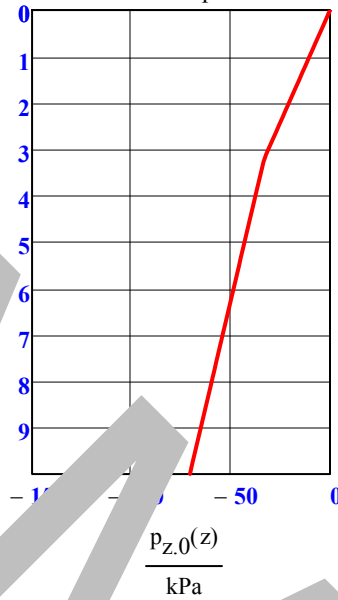
3.1.2. Graphs

Retained side

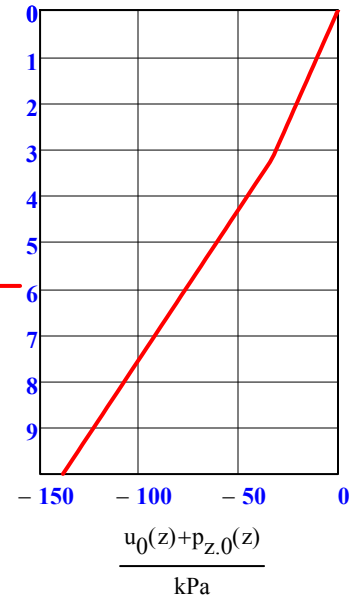
Water pressure



At rest earth pressure

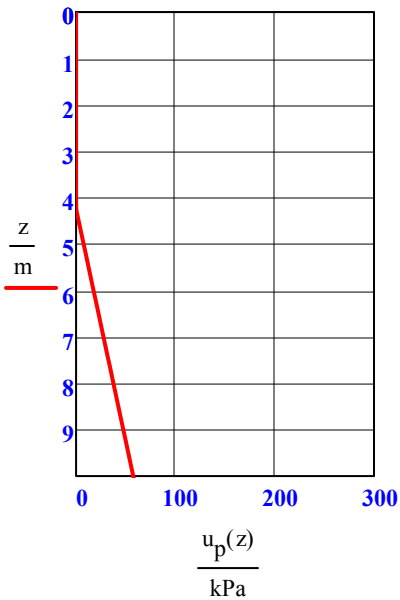


At rest earth pressure +
Water pressure

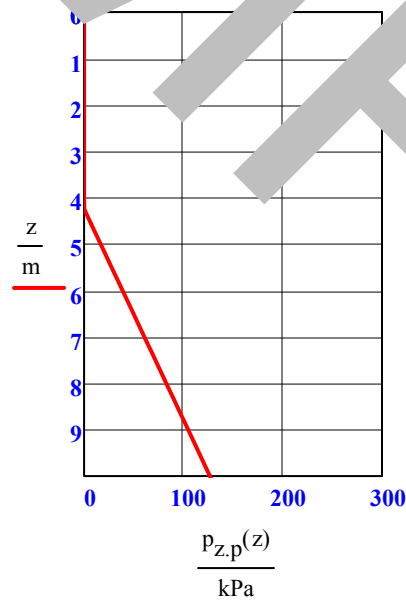


Resisting side

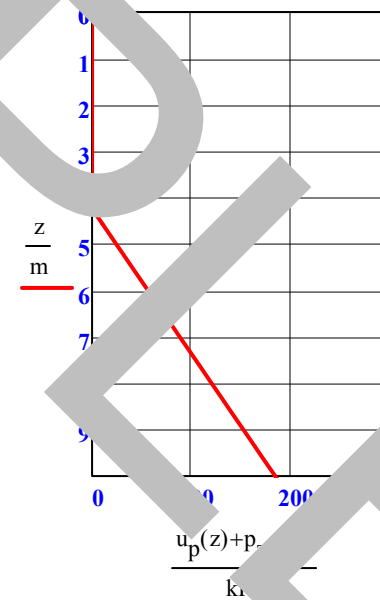
Water pressure



Passive earth pressure



Passive earth pressure +
Water pressure





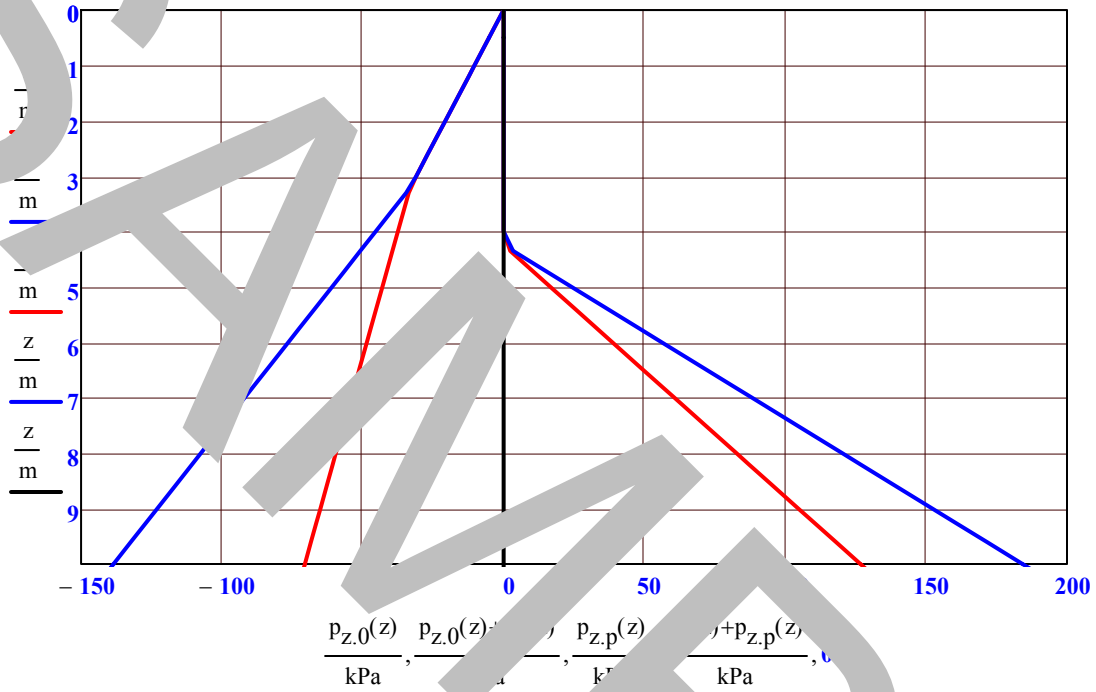
In a joint diagram

Retained side

Resisting side

Blue: At rest earth pressure +
Water pressure
Red: At rest earth pressure

Blue: Passive earth pressure +
Water pressure
Red: Passive earth pressure





3.2. Design calculation - southern side

2.2.1. Figure of horizontal loads

Pressure on the retaining side:

$$ret(z) := p_{z,0}(z) + u_0(z) + p_s(z)$$

Pressure on the resisting side:

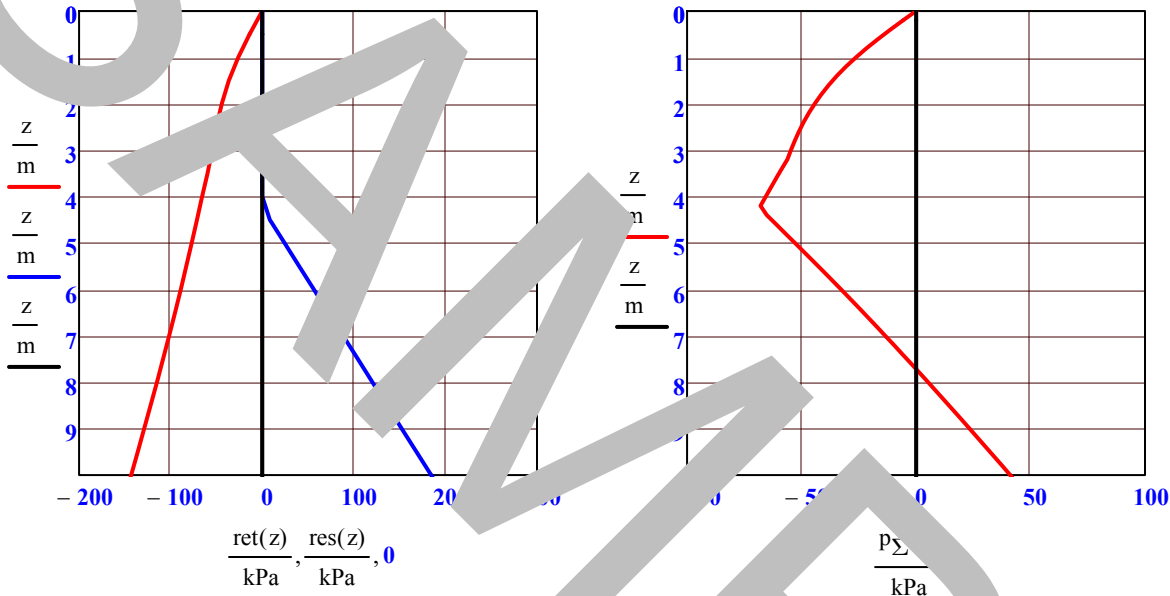
$$res(z) := p_{z,p}(z) + u_p(z)$$

Resultant of the two actions:

$$p_{\Sigma}(z) := res(z) + ret(z)$$

Retaining side Resisting side

The sum of the pressures acting on the wall.



The depth at which the pressure becomes zero:

$$z_1 := \text{root}(p_{\Sigma}(z), \text{var } z), \text{value } 7.719 \text{ m}$$

3.2.2. Depth of embedment

3.2.2.1. Anchor force (horizontal equilibrium)

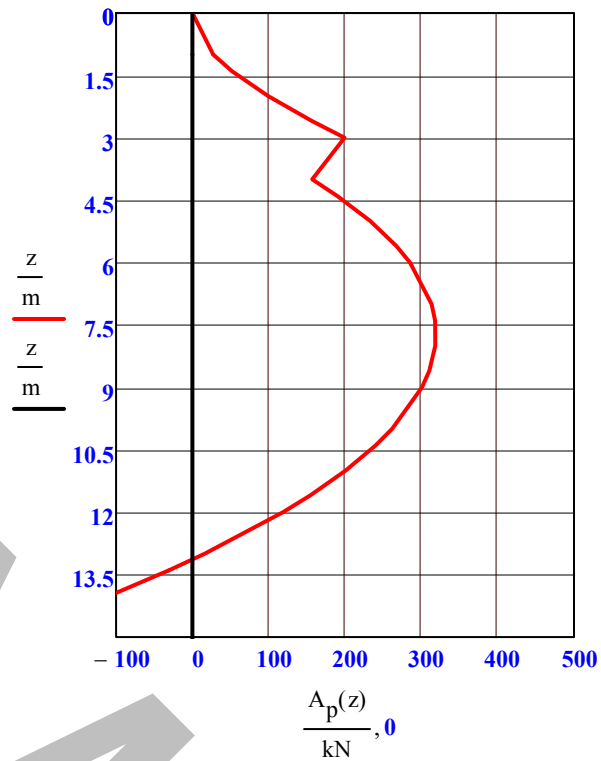
The force in the anchor equals to the negative resultant of the distributed loads:

$$A_p(z) := \begin{cases} \left[\left(- \int_0^z p_{\Sigma}(t) dt \right) \cdot X \right] & \text{if } z \leq H_2 \\ \left[\left(- \int_0^{H_2} p_{\Sigma}(t) dt \right) \cdot X - \left(\int_{H_2}^{z_1} p_{\Sigma}(t) dt \right) \cdot \Phi - \left(\int_{z_1}^z p_{\Sigma}(t) dt \right) \cdot 2\Phi \right] & \text{if } z > H_2 \end{cases}$$



The depth at which the resultant of the pressure becomes zero is:

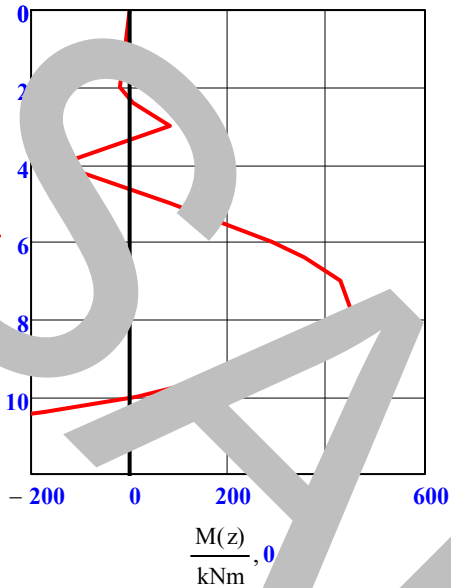
$$z_2 := \text{root}(p_{\Sigma}(z), \text{var } z) = 13.141 \text{ m}$$



3.2.2.2. Depth of embedment (bending moment at the bottom)

The bending moment for a cross section at depth "z":

$$M(z) := \begin{cases} \left[\int_0^z p_{\Sigma}(t)(z-t) dt \right] \cdot X + \begin{cases} 0 & \text{if } z < H_t \\ A_p(z) \cdot (z - H_t) & \text{otherwise} \end{cases} & \text{if } z \leq H_2 \\ \left[\int_0^{H_2} p_{\Sigma}(t) \cdot (z-t) dt \right] \cdot X + \left[\int_{H_2}^{z_1} p_{\Sigma}(t) \cdot (z-t) dt \right] \cdot \Phi + \left[\int_{z_1}^z p_{\Sigma}(t) \cdot (z-t) dt \right] \cdot \Phi + A_p(z) \cdot (z - H_t) & \text{if } z > H_2 \end{cases}$$



Length of soldier pile equals to the coordinate where $M(z)$ becomes zero:

$$L_{w_2} := \text{root}(M(\text{var}), \text{var}) = 10.037 \text{ m}$$

Applied wall length:

$$L_{\text{app.w}_2} := \text{ceil}\left(\frac{L_{w_2}}{0.1\text{m}}\right) \cdot 0.1\text{m} \quad L_{\text{app.w}_2} = 10.1 \text{ m}$$

Depth of the embedment shall be at least 3m according to the "Design Criteria" (23.pt.):

$$D_2 = \max(L_{\text{app.w}_2} - H_{d_2}, 3\text{m}) \quad D_2 = 6.77 \text{ m} \quad \text{"Design Criteria" 23.pt.}$$

3.2.3. Maximum bending moment

Bending moment:

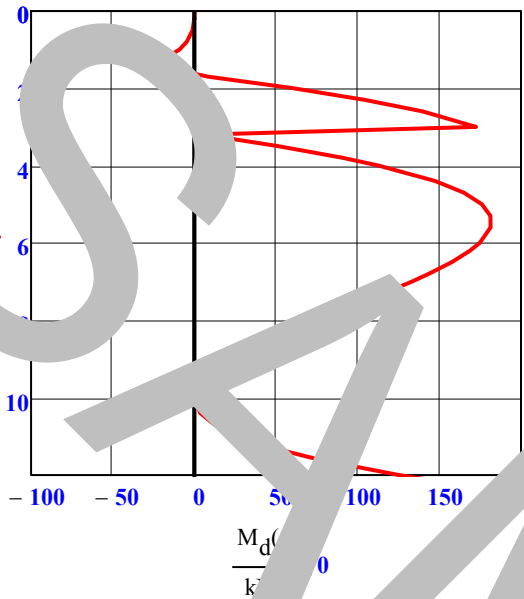
$$M_d(z) := \begin{cases} \left[\int_0^z p_{\Sigma}(t)(z-t) dt \right] \cdot X + \begin{cases} 0 & \text{if } z < H_t \\ A_p(L_{w_2}) \cdot (z - H_t) & \text{otherwise} \end{cases} & \text{if } z \leq H_2 \\ \left[\int_0^{H_2} p_{\Sigma}(t) \cdot (z-t) dt \right] \cdot X + \left[\int_{H_2}^{z_1} p_{\Sigma}(t) \cdot (z-t) dt \right] \cdot \Phi + \left[\int_{z_1}^z p_{\Sigma}(t) \cdot (z-t) dt \right] \cdot 2\Phi + A_p(L_{w_2}) \cdot (z - H_t) & \text{if } z > H_2 \end{cases}$$

Shear force:

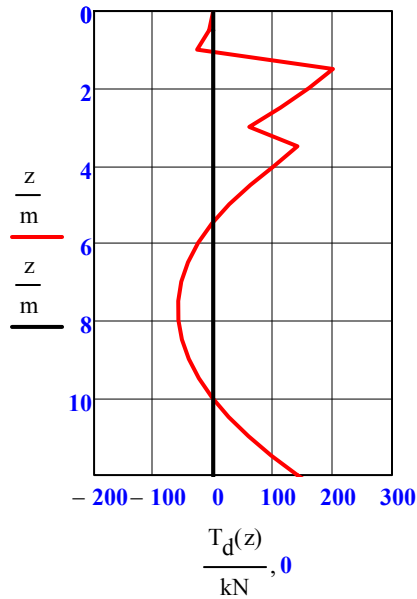
$$T_d(z) := \begin{cases} \left[\int_0^z p_{\Sigma}(t) dt \right] \cdot X + \begin{cases} 0 & \text{if } z < H_t \\ A_p(L_{w_2}) & \text{otherwise} \end{cases} & \text{if } z \leq H_2 \\ \left[\int_0^{H_2} p_{\Sigma}(t) dt \right] \cdot X + \left[\int_{H_2}^{z_1} p_{\Sigma}(t) dt \right] \cdot \Phi + \left[\int_{z_1}^z p_{\Sigma}(t) dt \right] \cdot 2\Phi + A_p(L_{w_2}) & \text{if } z > H_2 \end{cases}$$



Moment diagram



Shear force diagram



The position of the maximum bending moment:

$$z_3 := \text{root}(T_d(\text{var}), \text{var}) = 5.455 \text{ m}$$

The maximum bending moment:

$$M_{\max_2} := M_d(z_3)$$

$$M_{\max_2} = 160 \text{ kNm}$$

Required section modulus:

$$W_{\text{nec}_2} := \frac{M_{\max_2}}{FS_{\text{sp}} F_y}$$

$$W_{\text{nec}_2} = 779356.9 \text{ mm}^3$$

Applied section: W360x51

Section modulus: $S_{x,360x51} := 796 \cdot 10^3 \text{ mm}^3$

Inertia: $I_{x,360x51} := 141 \cdot 10^6 \text{ mm}^4$

Area: $A_{360x51} := 6450 \text{ mm}^2$



3.2.4. Anchor pull

The calculated magnitude:

$$A_2 := A_p \left(\frac{F_{pd,tot.s}}{F_{allow}} \right) = 259.576 \cdot \text{kN}$$

The maximum allowable load of a strand:

$$F_{allow} := \frac{F_{pu}}{FS} = 130 \cdot \text{kN}$$

"Design Criteria"
16.pt.

Required number of strands per tendon:

$$n_{a2} := \left\lceil \frac{A_2}{F_{allow}} \right\rceil = 2$$

$$n_{a2} = 2$$

3.2.5. Total design load of the tie back

$$F_{pd,tot.s} := A_2 = 259.576 \cdot \text{kN}$$

Lock-off load of a tendon: (ref: "Construction Procedure")

$$F_{pl} := 1.1 \cdot F_{pd,tot.s} = 286 \cdot \text{kN}$$

Proof load of a tendon: (ref.: "Construction Procedure")

$$F_{pp} := 1.33 \cdot F_{pd,tot.s} = 345 \cdot \text{kN}$$

3.2.6. Total amount of load on the shoring for one meter length (excavated height)

3.2.6.1. Due to soil

At rest earth pressure:

$$f_{p,0_1} := \int_0^{H_{d2}} p_{z,0}(t) dt = -57.35 \cdot \frac{\text{kN}}{\text{m}}$$

"Design Criteria"
22.1.pt.

3.2.6.2. Due to train load

$$f_{q_1} := \int_0^{H_{d2}} p_s(t) dt = -60.653 \cdot \frac{\text{kN}}{\text{m}}$$

"Design Criteria"
22.2.pt.

3.2.6.3. Due to hydrostatic pressure

$$f_{u_1} := \int_0^{H_{d2}} u_0(t) dt = -0.072 \cdot \frac{\text{kN}}{\text{m}}$$

"Design Criteria"
22.3.pt.



4. FE MODEL

The Finite Element Model is calculated using the Plaxis 8.2. software.
 The name of the file is 2012-01-26_soldier_pile.plx.

The Plaxis geotechnical finite element software is capable of modeling soil-structure interaction, and handling tie-backs, anchors properly, as points which have nonzero deflection.

"Design Criteria"
14.pt.

The software is generally used for plane strain problems. Taking into consideration that the shoring wall has a tributary width of: H_t above excavation level and $\Phi=0.61\text{m}$ below excavation level, the elastic modulus of the soil which is resisting to the movement of the soldier pile has to be decreased. The ratio of the decrease is the ratio of the two tributary width.

4.1. Geometry

Height of the

$$L_{\text{app.w}} = \begin{pmatrix} 8.8 \\ 10.1 \end{pmatrix} \text{ m}$$

Depth of the embedment:

$$\begin{pmatrix} 5.99 \\ 6.77 \end{pmatrix} \text{ m}$$

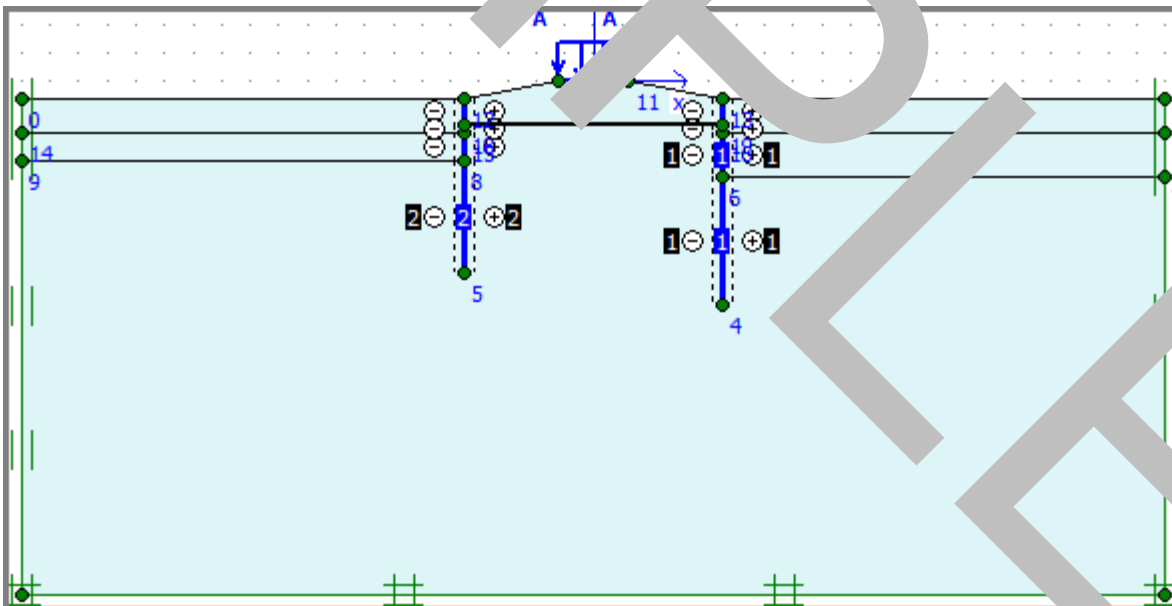
Excavation depths (design values):

$$D_{\text{ex.1}} := H_t + 30\text{cm}$$

$$D_{\text{ex.1}} = 1.30 \text{ m}$$

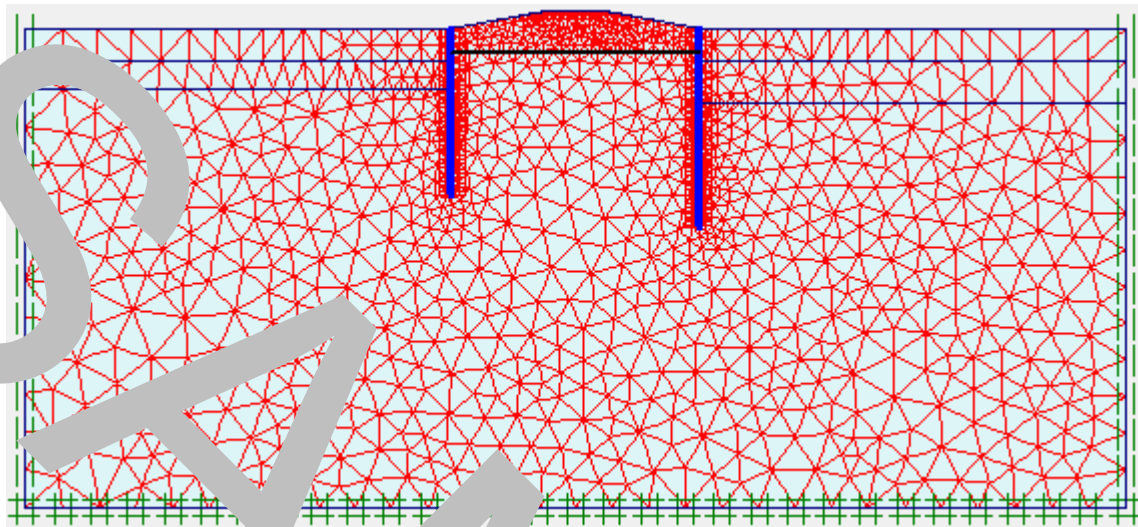
$$D_{\text{ex.2}} := H_d$$

$$D_{\text{ex.2}} = 3.33 \text{ m}$$





4.2. The mesh



4.3. Loads

4.3.1. Live load

Magnitude:

$$q_s = 1 \cdot 51 \cdot \frac{\text{kN}}{\text{m}^2}$$

Length:

$$s = 2.438$$

4.3.2. Anchorage

Calculated design load of a tendon:

$$A_p := \max(F_{pd.tot.n}, F_{pd.tot.s})$$

$$A_p = 259.576 \cdot \text{kN}$$

The more sophisticated FE model indicates that the soldier pile does not behave like a rigid body, therefore in order to reduce the top displacement the tieback prestressing force should be increased.

Reduced prestressing force of one tendon:

$$F_{app} := 20\% \cdot A_p = 51.915 \cdot \text{kN}$$

Spacing of tendons (equals to spacing of soldier piles):

$$s_{app.a} := X = 2 \text{ m}$$

Unit prestress force to be used in FE model:

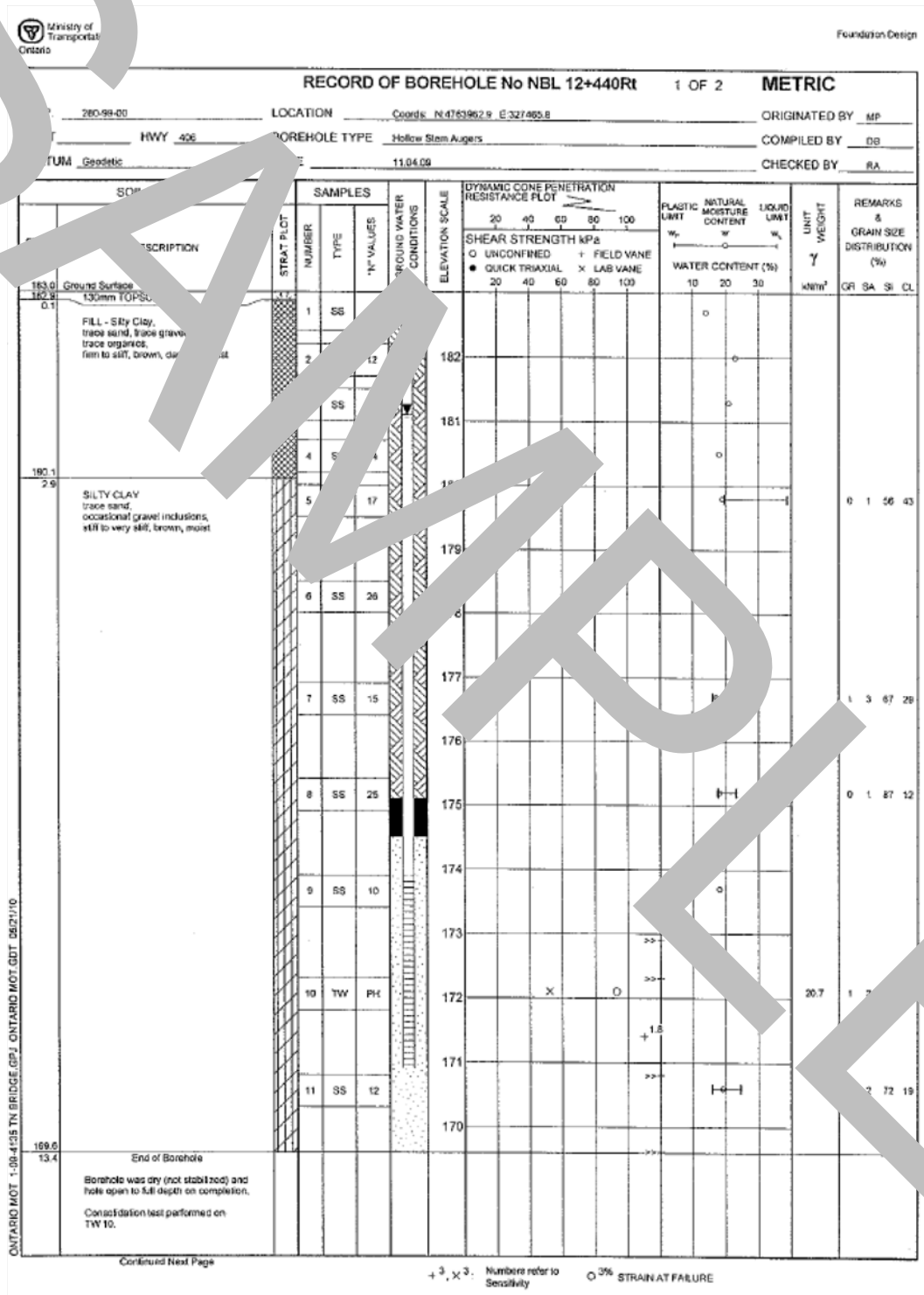
$$f_d := \frac{F_{app}}{s_{app.a}} = 25.958 \cdot \frac{\text{kN}}{\text{m}}$$



4.4. Material properties

4.4.1. Soil

We take NBL 12+440 borehole (Terraprobe soil report (*File No. 1-09-4135*)) as the basis of soil properties.

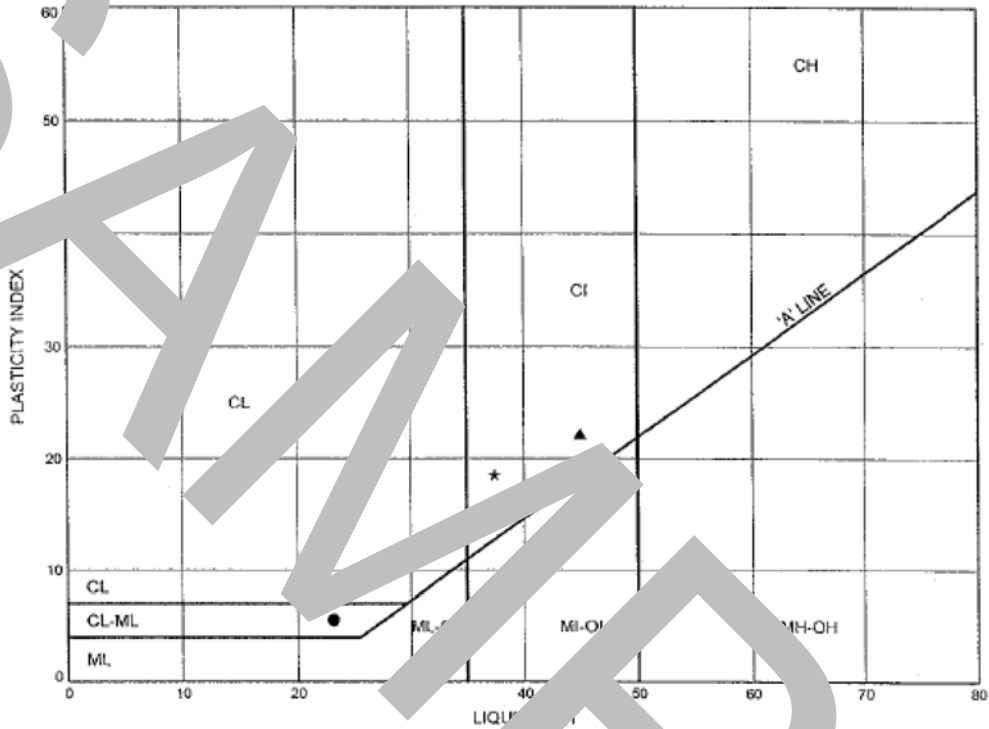




ATTERBERG LIMITS TEST RESULTS

FIGURE B11

SILTY CLAY



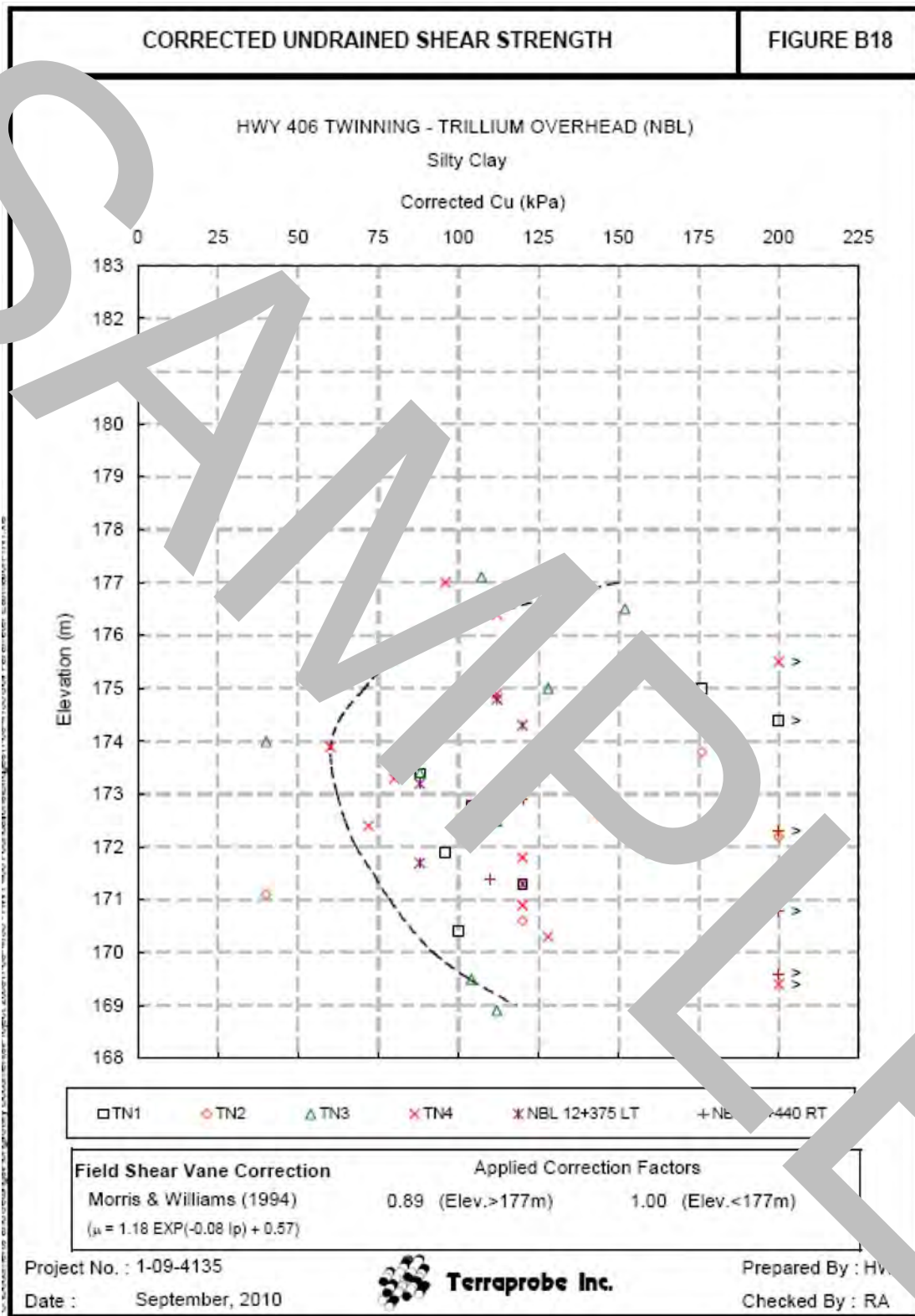
SYMBOL	BOREHOLE	DEPTH (m)	ELEVATION (m)
●	NBL 12+440rt	7.8	175.2
⊠	NBL 12+440rt	12.4	170.6
▲	TN1	2.5	181.0
★	TN1	4.7	178.0
⊙	TN1	7.8	175.2
⊖	TN1	10.9	172.1

ALTR 1-09-4135 TN BRIDGE.GPJ 05/18/10

Date May 2010
 Project 1-09-4135



Prep'd
 Chkd.





Cinder fill material with organics overlying silty clay.

Unit weight of moist soil: $\gamma_{moist} := 20.7 \frac{kN}{m^3}$

Unit weight of submerged soil: $\gamma_{subm} := 21 \frac{kN}{m^3}$

The Mohr-Coulomb plasticity criteria is used.

Strength	
E_{ref} : <input type="text" value="2,500E+04"/>	c_{ref} : <input type="text" value="60,000"/> kN/m ²
ν (nu): <input type="text" value="0.35"/>	ϕ (phi): <input type="text" value="30,000"/> °
	ψ (psi): <input type="text" value="0"/>
Alternatives	
G_{ref} : <input type="text" value="9259,259"/> kN/m ²	V_s : <input type="text" value="65,730"/> m/s
E_{oed} : <input type="text" value="4,012E+04"/> kN/m ²	V_p : <input type="text" value="136,800"/>

Material properties of soil

Young's modulus: (based on plasticity index, liquid limit, plastic limit) $E_{ref} = 25000 \frac{kN}{m^2}$

We assumed no friction between soil and shoring wall:

Decreased Young's modulus: $E_{decreased} = E_{ref} \cdot \frac{2}{X} = 15250 \frac{kN}{m^2}$

"Design Criteria" 27.pt.

Poisson coefficient (Typical average value for clay): $\nu := 0.35$

Cohesion (min. of statistical evaluation): $c_{ref} := 60 \frac{kN}{m^2}$

Angle of inner friction (based on the given passive earth pressure coefficient): $\phi := 30^\circ$

4.4.2. Anchor

Axial stiffness of the tendons:

$n_{app} := \max(n_{a1}, n_{a2}) = 2$

$EA_t := E_s \cdot n_{app} \cdot A_s$ $EA_t = 55999.888 \cdot kN$



4.4.3. Wall

Stiffness of W360x33:

Axial: $EA_s := E_s \cdot A_{360x33} = 834000 \cdot \text{kN}$

$$\frac{EA_s}{X} = 417000 \cdot \frac{\text{kN}}{\text{m}}$$

Bending: $EI_s := E_s \cdot I_{x,360x33} = 16540 \cdot \text{kN} \cdot \text{m}^2$

$$\frac{EI_s}{X} = 8270 \cdot \frac{\text{kN} \cdot \text{m}^2}{\text{m}}$$

W360x51

Axial: $EA_s := E_s \cdot A_{360x51} = 1245000 \cdot \text{kN}$

$$\frac{EA_s}{X} = 645000 \cdot \frac{\text{kN}}{\text{m}}$$

Bending: $EI_s := E_s \cdot I_{x,360x51} = 20000 \cdot \text{kN} \cdot \text{m}^2$

$$\frac{EI_s}{X} = 14100 \cdot \frac{\text{kN} \cdot \text{m}^2}{\text{m}}$$

4.5. Construction stages

Identification	Phase	Start from	End at	Loading input
Initial phase	0	0	N/A	N/A
✓ Load	1	0	1	Elastic Staged construction
✓ Load+Ex1	2	1	2	Elastic Staged construction
✓ Load+Ex1+Anch	3	2	3	Plastic Staged construction
✓ Load+Ex2+Anch	4	3	4	Plastic Staged construction
✓ Anch+Ex1	5	0	5	Plastic Staged construction

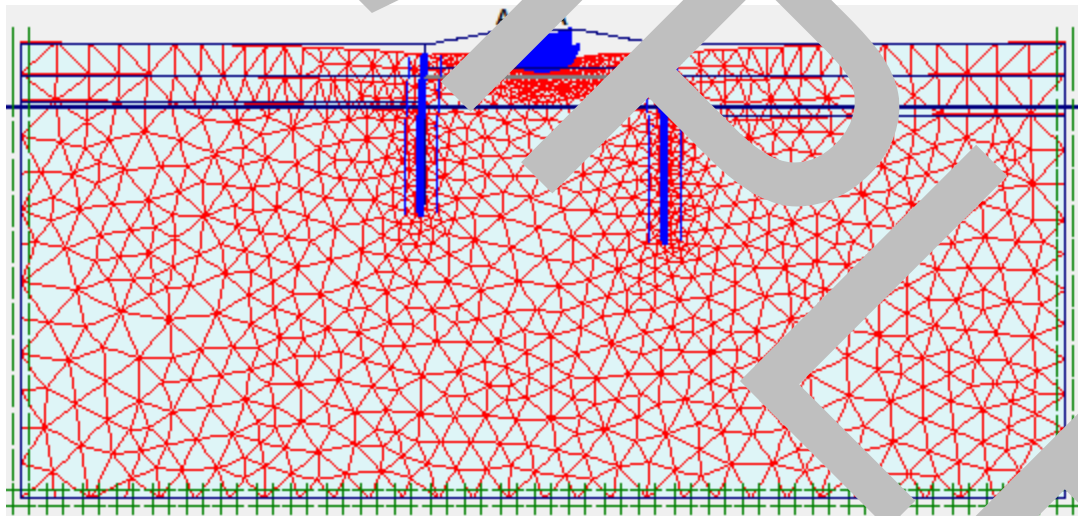
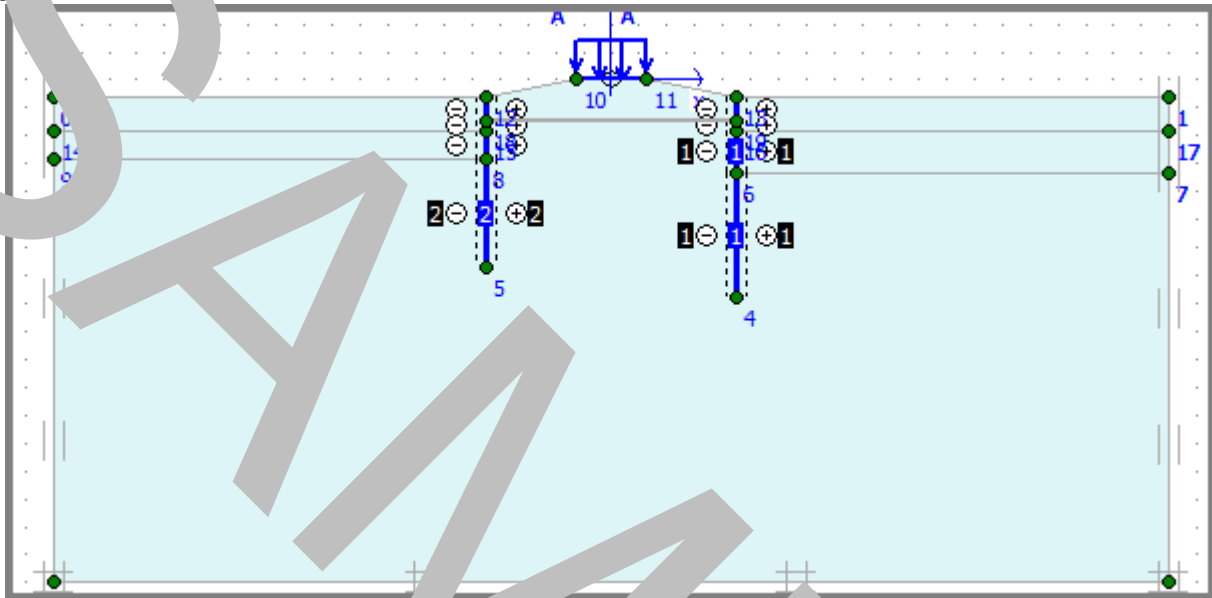
"Design Criteria"
3. 5. 14. pt.



4.5.1. Phase 1

The wall is driven in,
Live load is applied,
No excavation

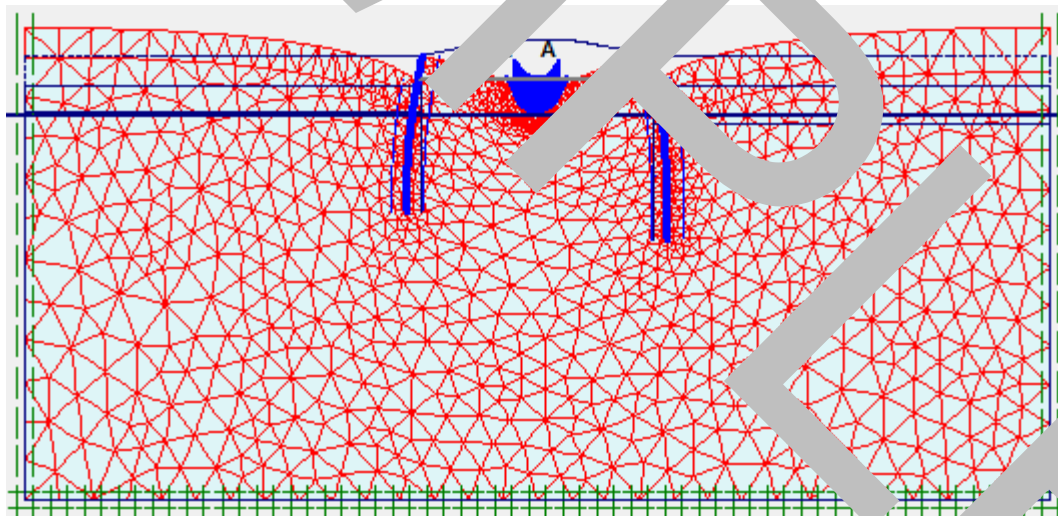
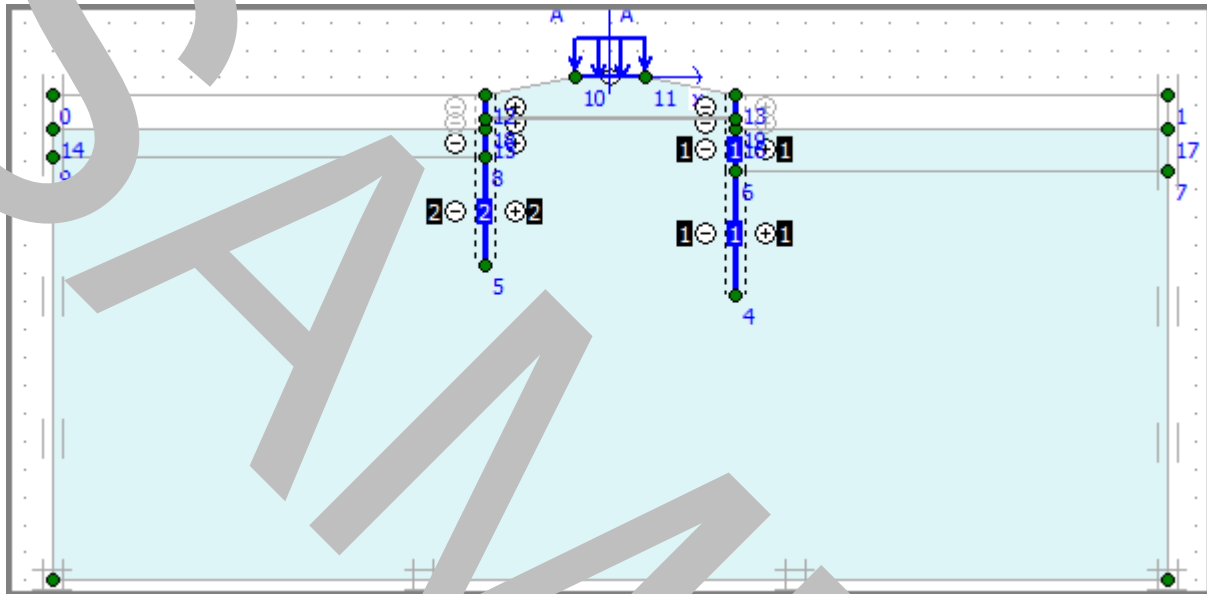
Starting from the initial condition.





4.5.2. Phase 2

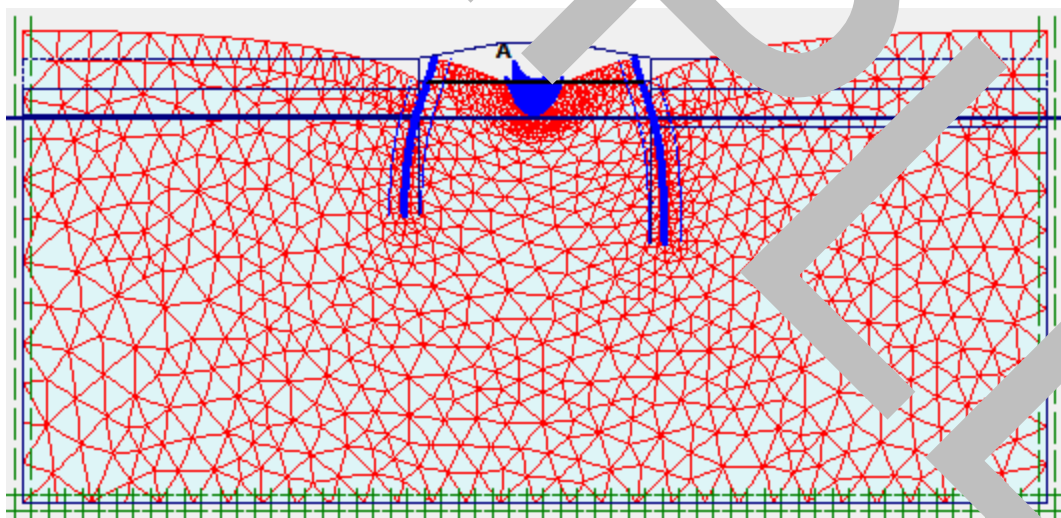
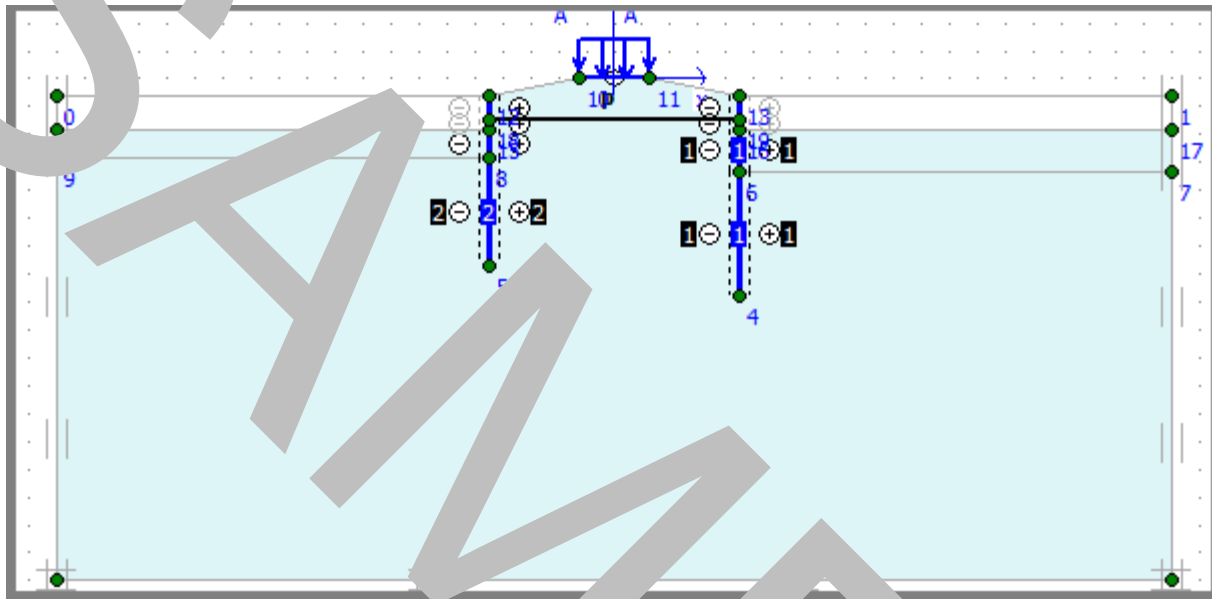
The wall is driven in,
 Live load is applied,
 Excavation to low anchorage level.
 Starting in Phase





4.5.3. Phase 3

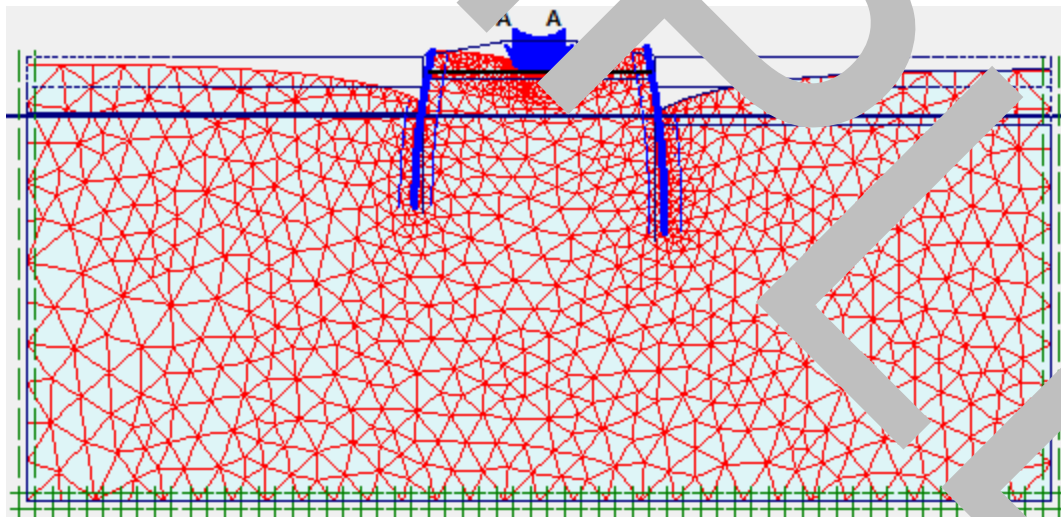
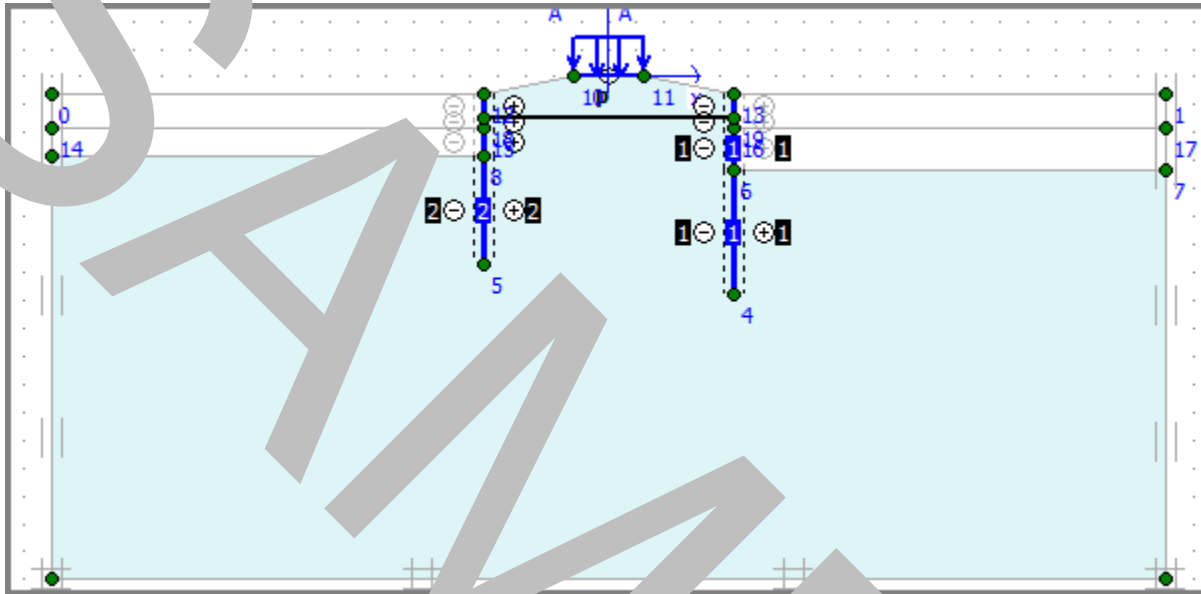
The wall is driven in,
 Live load is applied,
 Excavation to low anchorage level.
 Anchor prestressing
 Starting from Phase 2.





4.5.4. Phase 4

The wall is driven in,
 Live load is applied,
 Excavation to the final level.
 Anchors are applied.
 Starting from Phase 3.

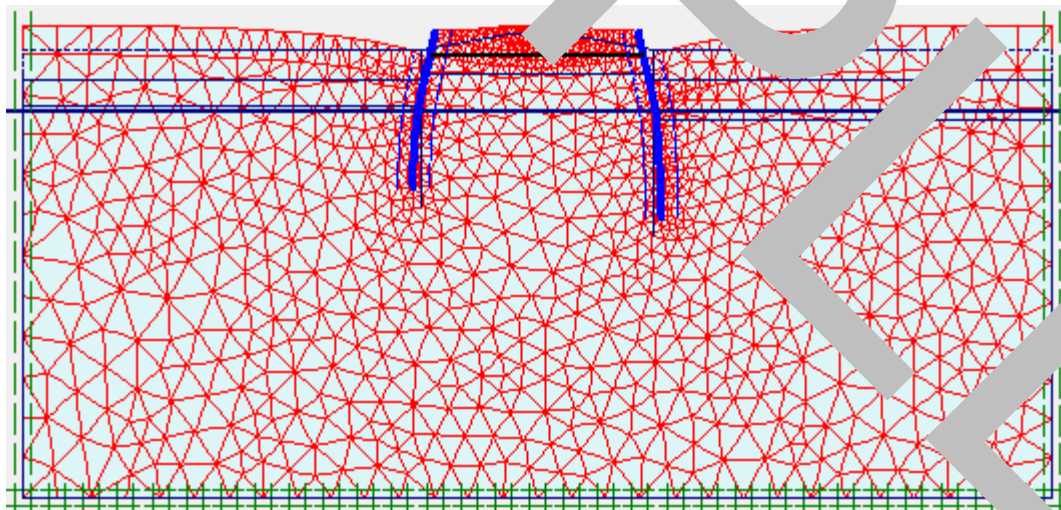
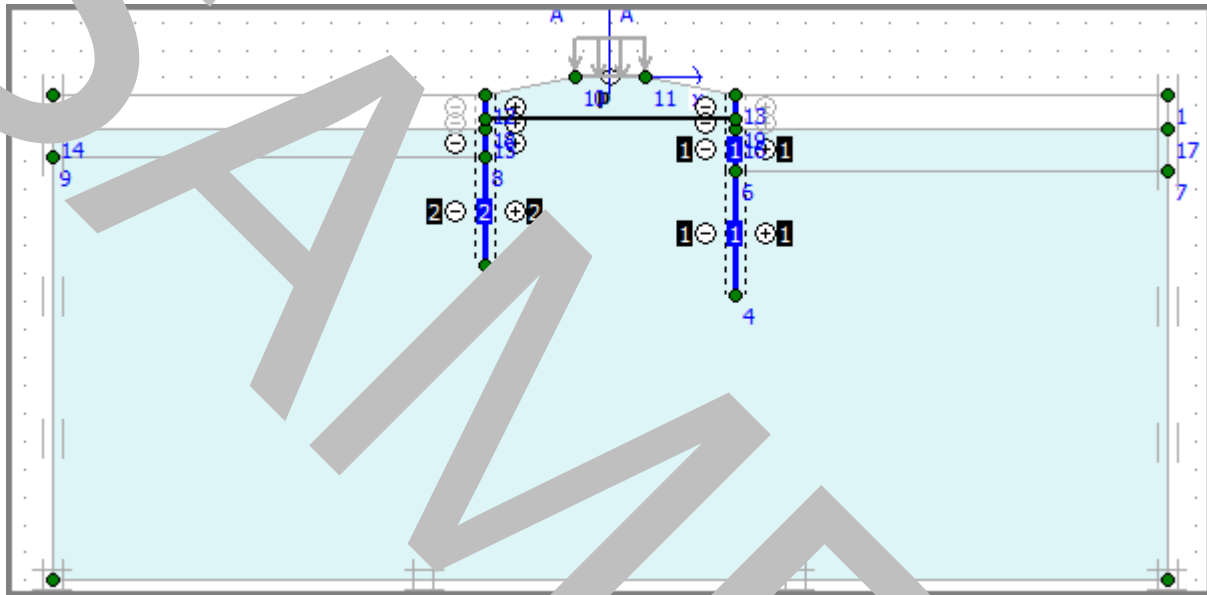




4.5.5. Phase 5

Control phase to check the soil without the load

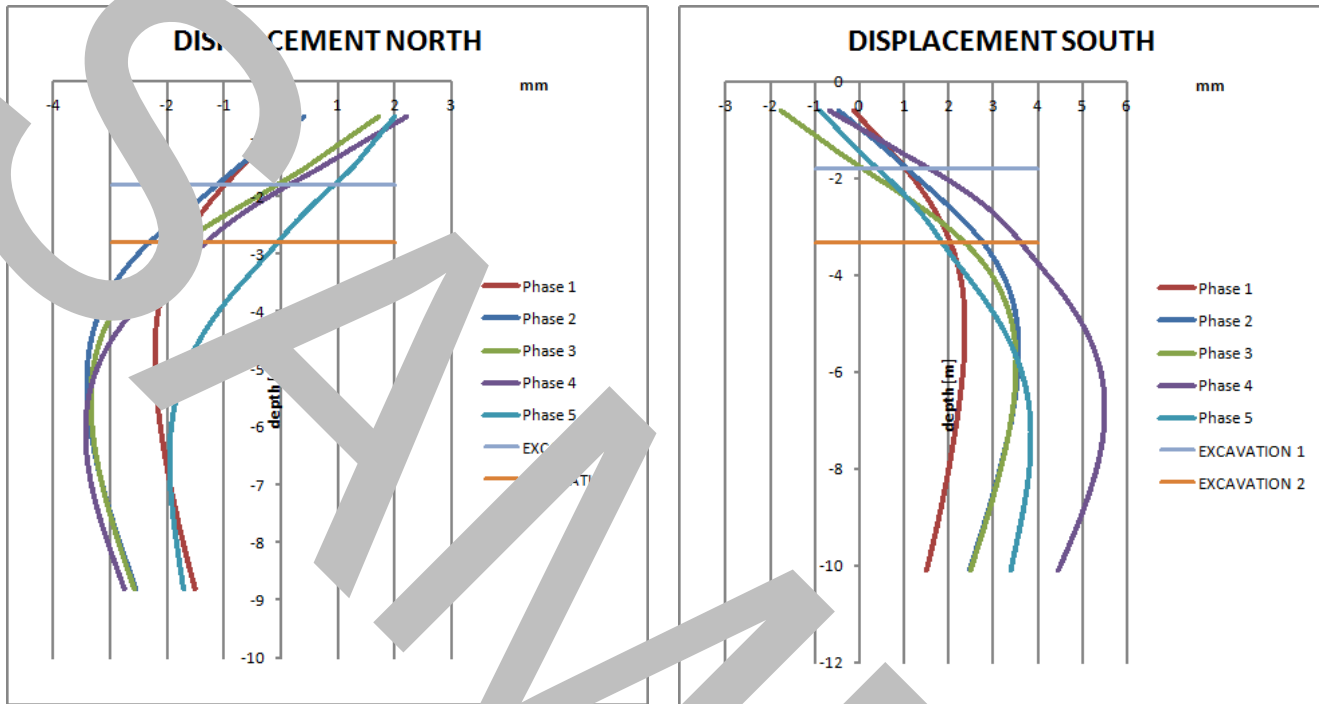
The wall is driven
 Live loads excluded
 Excavated to the final level.
 Anchors applied.
 Starting from the initial phase.





4.6. Results

4.6.1. Displacements



The lateral displacements are limited to the 0.1% of the excavation height in Phases 1-4.

$$\Delta s_{\max} := 0.001 \cdot H_{d_2} = 3.33 \cdot \text{mm}$$

"Design Criteria"
15. pt.

The maximum displacement satisfies this criteria, and we can still the requirement of displacement (5mm) while the tiebacks are being stressed (Phase 5).

"Design Criteria"
30. pt.

4.6.2. Check of soil's plastic resistance in prestressing phase

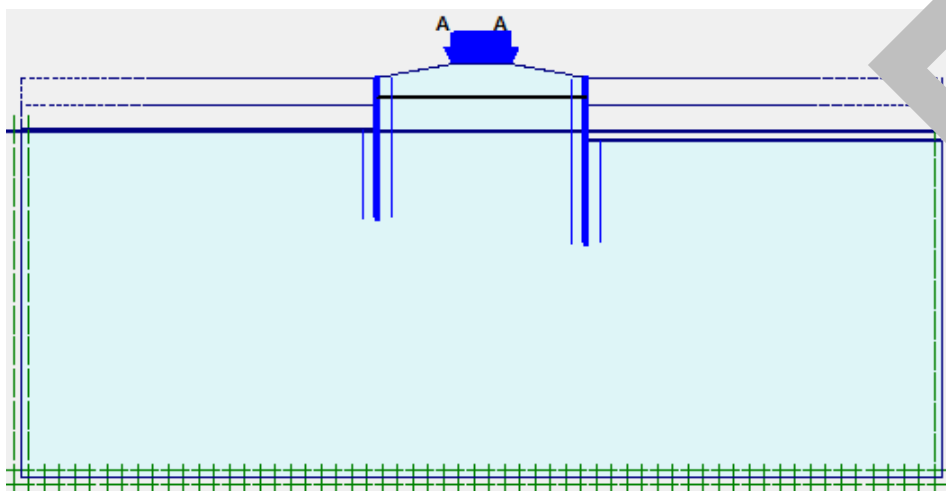


Figure shows prestressing phase. Red squares would represent plastic points on the face of the soil. No plasticity is present because of prestressing.

"Design Criteria"
6. pt.



5. Summary

5.1. Soldier pile

Height of the soldier pile:

$$L_{\text{app.w}} = \begin{pmatrix} 8.8 \\ 10.1 \end{pmatrix} \text{ m}$$

Depth of the embedment:

$$D = \begin{pmatrix} 5.99 \\ 6.77 \end{pmatrix} \text{ m}$$

Section:

South side: W360x51

North side: W360x33

5.2. Tie-back

Number of strands in a tendon:

$$n_{\text{app}} = 2$$

Spacing:

$$s_{\text{app.a}} = 2 \text{ m}$$

Design load of a tendon:

$$A_p = 260 \cdot \text{kN}$$

Prestressing force of the tendons:

$$F_{\text{app}} = 51.915 \cdot \text{kN}$$

Lock-off load of a tendon:

(ref.: "Construction Procedure")

$$F_{\text{pl}} := F_{\text{app}} \quad F_{\text{pl}} = 51.915 \cdot \text{kN}$$

Proof load of a tendon:

(ref.: "Construction Procedure")

$$F_{\text{pp}} := 1.33 \cdot F_{\text{app}} \quad F_{\text{pp}} = 69.047 \cdot \text{kN}$$

Note: The lock-off load and the proof load are calculated based on the applied prestressing force rather than the design load. This is the result of the restriction for the displacement criteria.